



凝聚态物理-北京大学论坛

2012年第4期

由拉曼光谱学揭示的 纳米半导体的新物理特性

**NOVEL PHYSICAL NATURE of NANO-SEMICONDUCTORS
EXPOSED by RAMAN SPECTROSCOPY**

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2012-03-15

周五论坛

低维 / 纳米半导体的曼光谱学与物性

北京大学 张树霖

第一讲

第一部分 拉曼光谱学基础

第二部分 低维结构及其拉曼光谱

第二讲

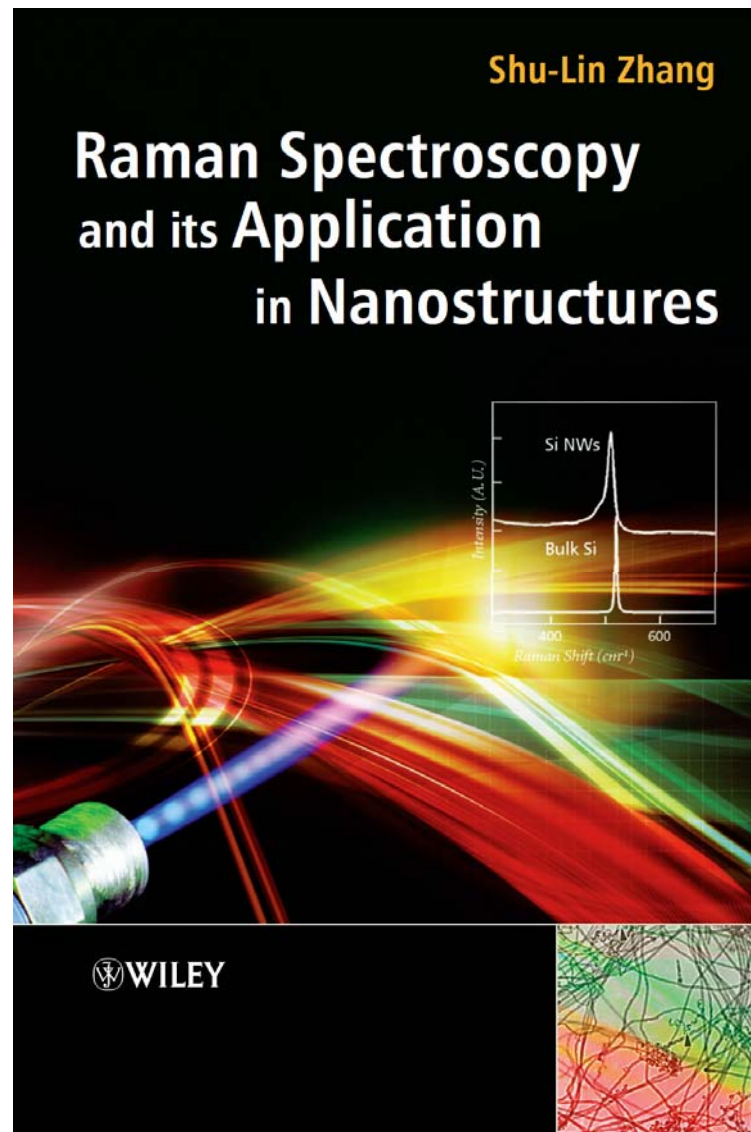
纳米半导体的拉曼光谱学与物性

北京大学 物理楼212

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II. Raman Spectral Feature of Nano-semiconductors

III. Abnormal Raman Spectral Feature Relative to Conventional Raman Spectroscopy.

IV. Abnormal Raman Spectral Feature Relative to Nanostructure Raman Spectroscopy

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I. Basic Feature of Raman Spectra and Nanostructures

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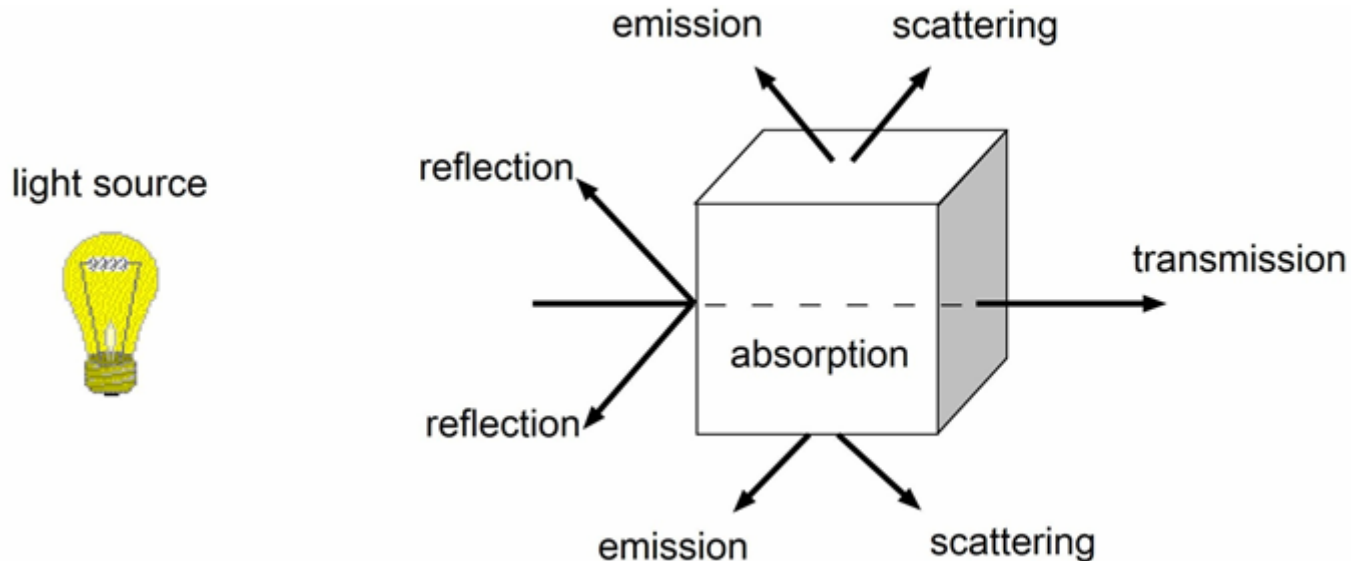
IV. Abnormal Raman Spectral Feature Relative to Nanostructure Raman Spectroscopy

I-1 Fundamentals of Raman Spectra

(I) Production of Spectrum

The spectrum is induced by the light irradiation on medium.

It produces some types of light:



(1) Scattering light is one of many types of light induced by irradiation

The **Light** induced by **monochromatic light** irradiation

- Reflected and transmitted light:
The frequency must be **same** with
that of **monochromatic light**.
- Scattering light:
The frequency can be **different** from
monochromatic light .

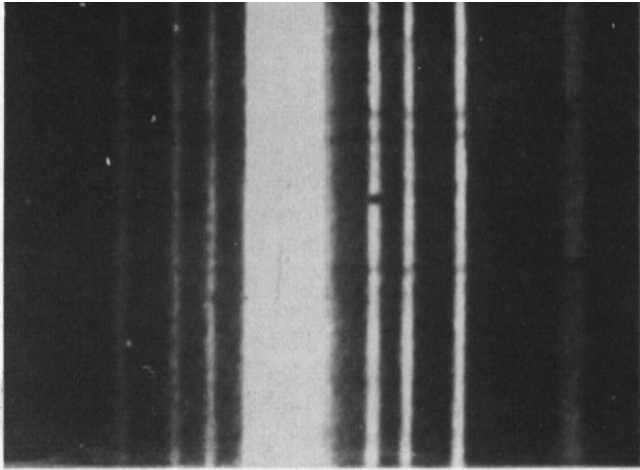
(2) Under monochromatic light irradiation:
The scattering light can behave as a spectrum,
while other two are impossible.

The frequency/energy of scattering light spectra

$\omega_S - \omega_{Rad} = \Delta\omega$	<i>Name</i>	<i>Property</i>
$> 1 \text{ cm}^{-1}$ elastic	Raman	Non-
$< 1 \text{ cm}^{-1}$	Brillouin	Elastic
$< 10^{-5} \text{ cm}^{-1}$	Rayleigh	Elastic (~ 0)

(3) Raman scattering spectrum is one type of light scattering spectra.

(II) Features of Raman scattering spectra



(1) Intensity I

- $I_{\text{Raman}} / I_{\text{Incident}} < 10^{-6 \sim 12}$
($I_{\text{Rayleigh}} / I_{\text{Incident}} < 10^{-3}$)
- $I_{\text{Stokes}} / I_{\text{Anti-Stokes}} \approx \exp(\hbar \omega_k / kT)$

>>

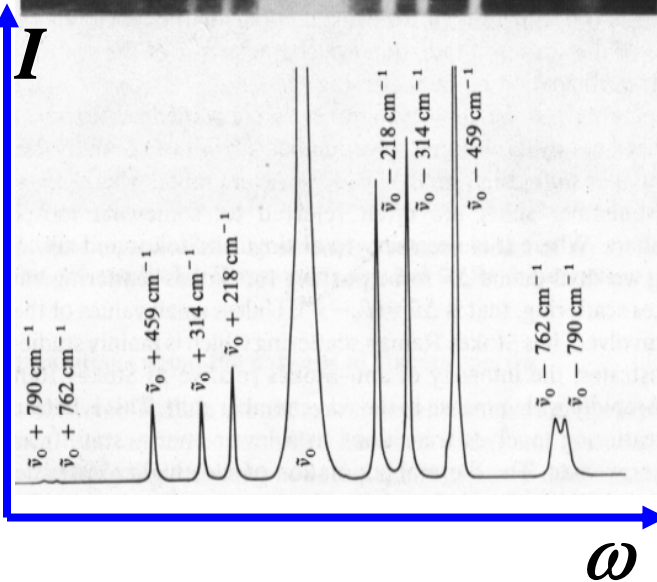
2) Frequency ω_S

- ω_S Independent of ω_i

Energy conservation

$$\omega_{\text{Stokes}} = \omega_{\text{Anti-Stokes}}$$

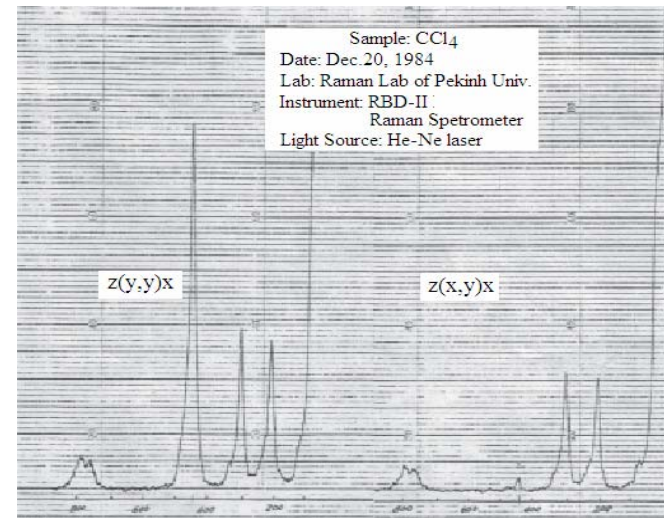
Time inversion symmetry



(3) Polarization P

Raman scattering light is polarized light,
If the orientation of the molecular or crystals is fixed.

- That is the Reflection of the symmetry properties of molecules or crystals;
- The information of symmetry of objects can be obtained from polarized Raman spectra.



(4) Spread direction K

As no relevance
between the phases of different Raman beams
The spread in space is isotropic.

Raman spectral features

- Raman spectrum is a non-elastic light scattering spectra with the energy/frequency $> 1 \sim 2 \text{ cm}^{-1}$.

- Raman spectrum is one of the spectra with unique spectral features in frequency, intensity, polarization and spread direction, such as, its frequency ω_S :

1. ω_S Independent of ω_i

2. $|\omega_{\text{Stokes}}| = |\omega_{\text{Anti-Stokes}}|$

I-2 Introduction to nanostructure/nanomaterial

1. The influence of size on physical law

The size of the object has a significant influence to the properties and movement rules of matters.

- A macro-scale ($>$ light wavelengths $\sim \mu\text{ m}$) material is generally considered to be an infinite system and comply with classical physics law;
- A micro-scale (subatomic scale) material is described by quantum physical law.

2. Definition of nanostructure/nanomaterial

- Ones usually define a structure/material with a small size of a sub-micron $\sim 1 \text{ nm}$ ($1 \sim 100 \text{ nm}$) in geometry as the nano-materials/nanostructures.
- For such defined nanostructure/nanomaterial, it is unable to determine which type of physical law will be complied, as its size is between the macroscopic and microscopic scales
- A scientific definition of the nano-structure/material:
macroscopic in geometrical size;
But appears the quantum mechanical phenomena.

3. Characteristic Length

- Following length called as 'Characteristic Length', such as

Dephasing length,
Diffused length
Bohr radius r_e ,
de Broglie wavelength

....

- The scale of same characteristic lengths might be different under different case. For example,
The de Broglie wavelength of electrons in the conduction band bottom can be from 10-100nm and the Bohr radius of the electrons in hydrogen atoms and conduction electrons Bohr radius are 0.05nm and 10 nm, respectively.

4. Essential effect of small sizes

(1) The small size of nanostructures/nano-materials induces a finite size effect (FSE).

The influence of FSE is more concerned in physics.

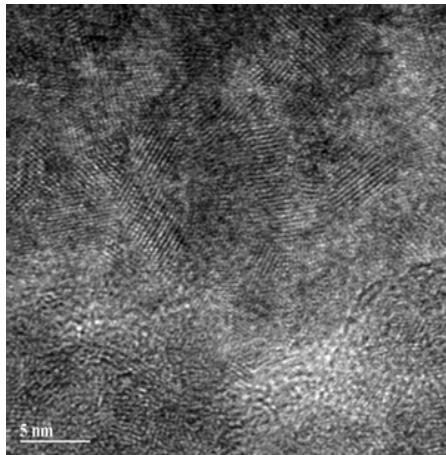
(2) The small size of nanostructures/nano-materials results in huge specific surface .

This play an more important role in chemical field.

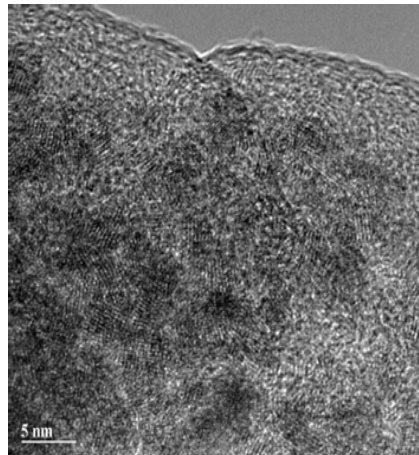
I-3 Nanostructured materials

1. Nanomaterial in nature and history

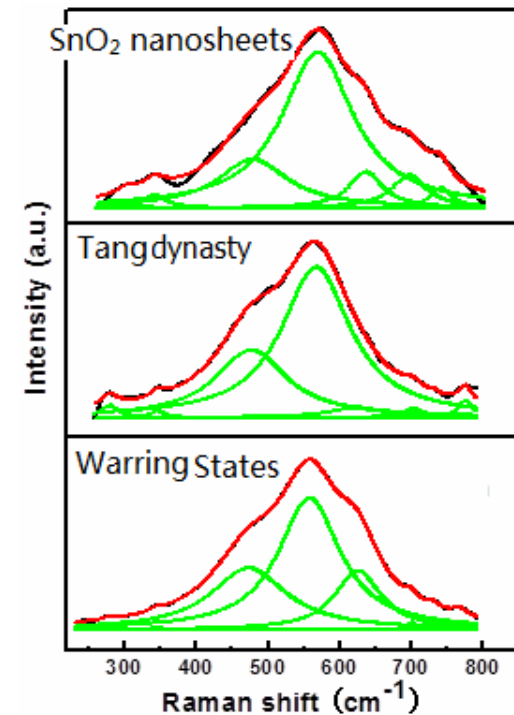
Nano materials already exists in nature and history. For example, the Chinese ink appeared more than 1000 years ago. In fact, it may be more early, such as, the ancient bronze mirror.



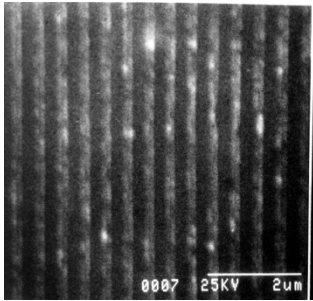
Warring states
bronze mirror



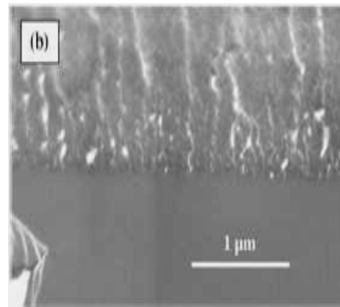
Tang dynasty
bronze mirror



2. Artificial Nanostructured materials



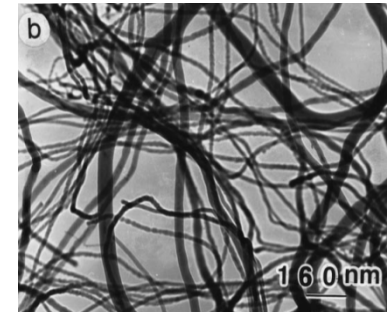
Superlattice



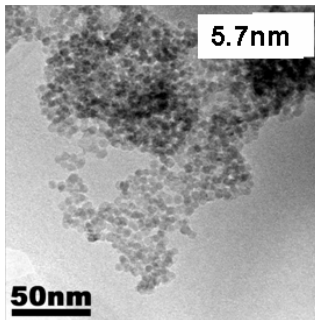
porous silicon



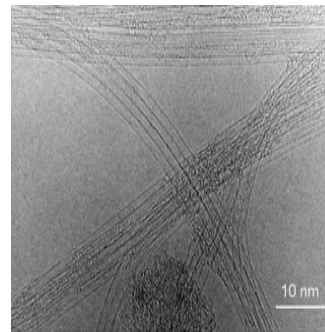
nano rod



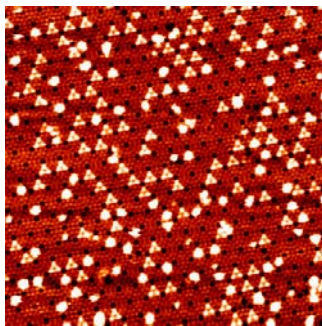
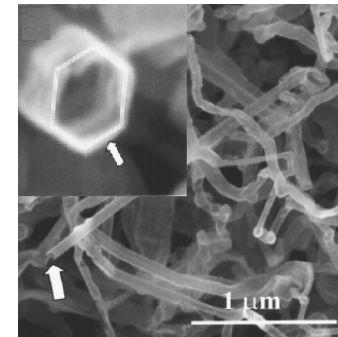
nano wires



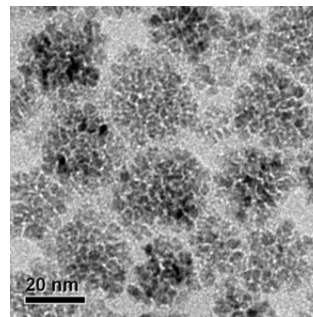
nano particle



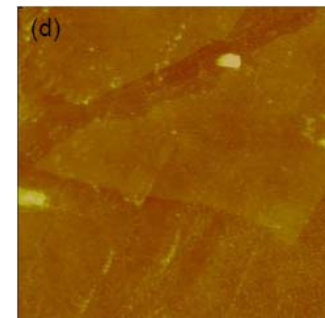
nano-tubes



cluster



nano flowers



graphne

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II. Raman Spectral Feature of Nano-semiconductors

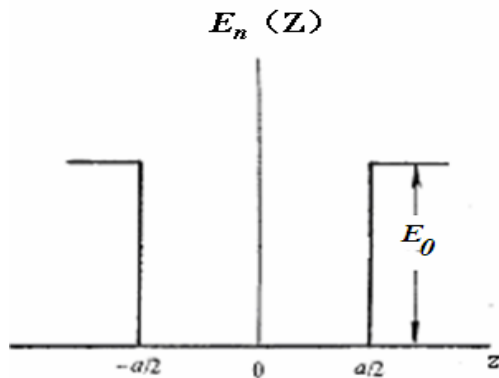
III. Abnormal Raman Spectral Feature Relative to Conventional Raman Spectroscopy.

IV. Abnormal Raman Spectral Feature Relative to Nanostructure Raman Spectroscopy

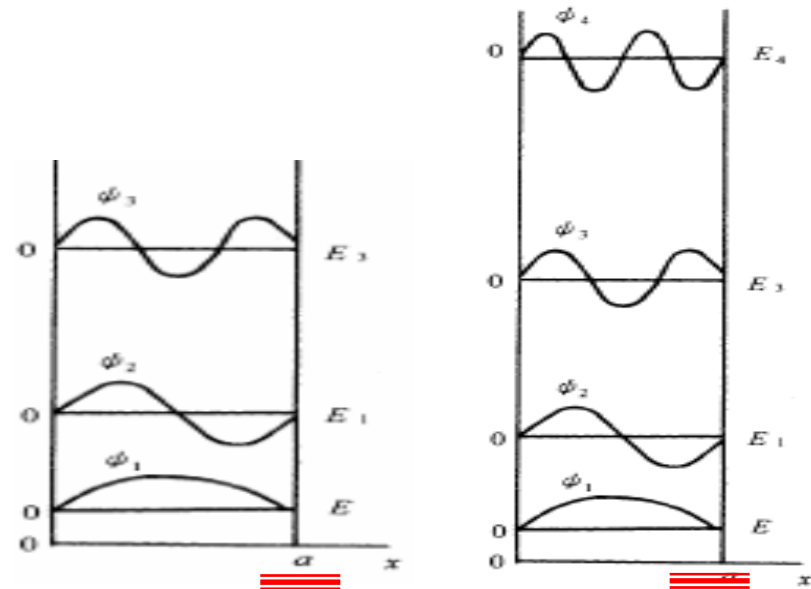
II-1 FSE on basic physical quantity

Finite size leads to an infinite and unconfined system becoming a limited and confined system.

(I) FSE on Energy-quantum confinement effect (QCE)



Energy level and wave function



$$E_n = \frac{n^2(\pi\hbar)^2}{2m} \frac{1}{a^2} \quad E_n(k) = E_n + \frac{\hbar^2 k^2}{2m}$$

Energy (Raman frequency) changes with sample sizes a

(II) FSE on Symmetry

1. Spatial symmetry - translation symmetry

In Bulk (infinite) semiconductors, there must have the **translation symmetry**



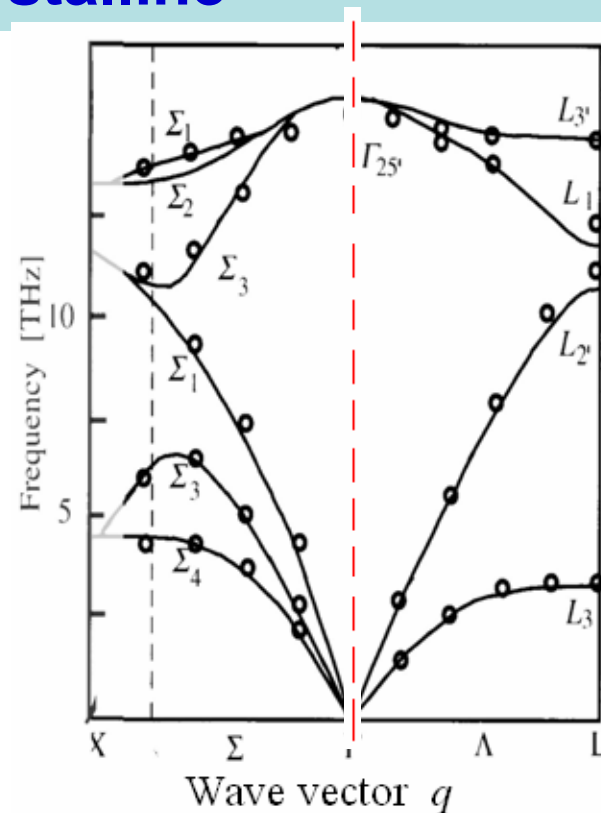
Long-range order ~ crystalline



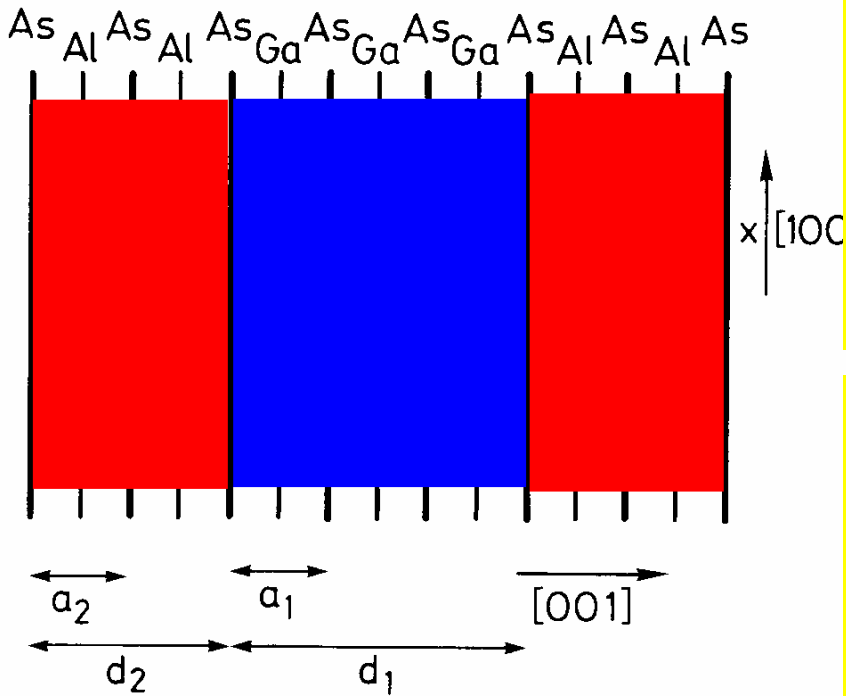
Momentum $h\mathbf{q}$ (wavevector \mathbf{q}) conservation



For visible Raman scattering means
wavevector selection rule
 $\mathbf{q} = 0$.



2. Crystallographic symmetry



- The **symmetry** of GaAs/AlAs SLs is changed

from

D_{4d} of GaAs and AlAs

to

T_d of GaAs and AlAs

- Correspondently, the **period** (~lattice constant) is

$$L = d_1 + d_2 = (n_1 + n_2)a$$

a - Lattice constant of GaAs and AlAs;

n_1 and n_2 - single layer number of GaAs and AlAs in SLs.

(III) FSE on Momentum

1. Uncertainty relation

$$\Delta k \Delta r \leq \hbar \quad i=x,y,z$$

$$\Delta k_i \Delta r_j \leq \hbar$$

When the size r is very small, the uncertainty of the momentum will be very big.

The momentum of phonons appears diffusion.

Since momentum diffusion



The phonons of wavevectors $\Delta \mathbf{q}$, rather than $\mathbf{q} = 0$ are possible to join Raman scattering scattering

II-2 FSE on Raman Features

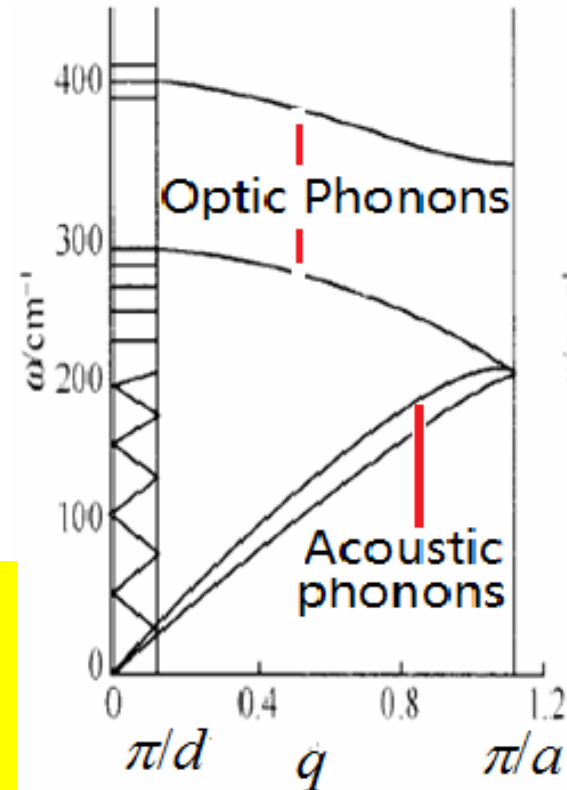
It can be described by the models setup on the change of physical quantity mentioned.

(I) Layered nanostructure materials-Superlattices (SLs)

- The big period $d = na$ of SLs has the large B-zoon of π/a changing as a small one of π/d .
- The bulk dispersion curve folded into a small zoon. Phonon energy is splitted into many sub-energy-levels in SLs.

Raman features of SLs

- (1) Active optic mode in bulks "split" into many sub-modes.
- (2) Forbidden acoustic become active.



(II) Non-layered nanostructure materials - Nanomaterials (NMs)

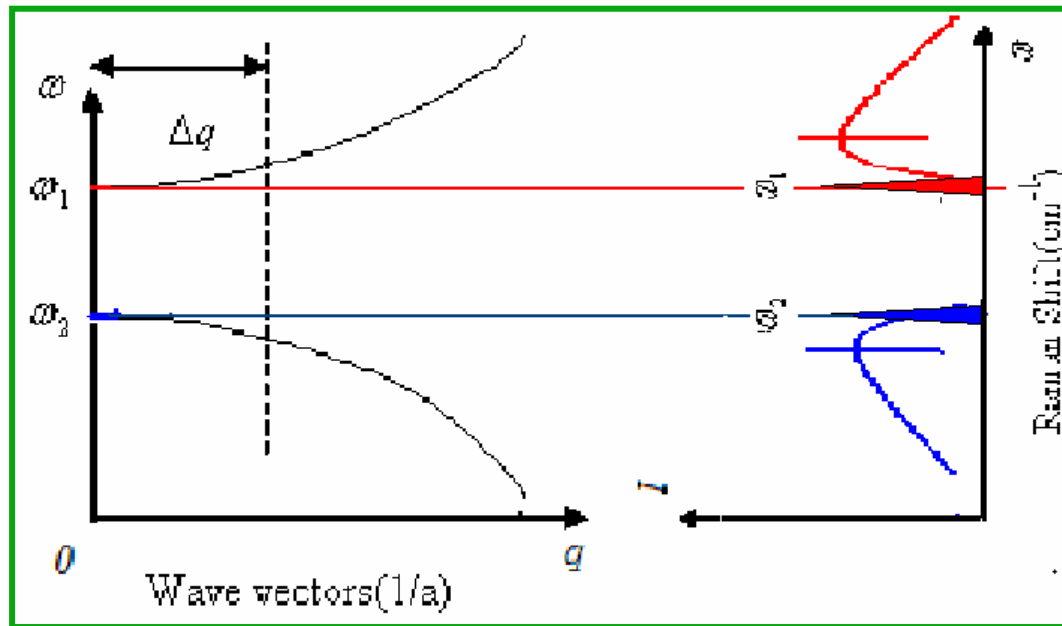
Microcrystal model (MCM)

Based on FSE on momentum and translation symmetry

$$q \neq 0 \text{ and } \Delta q \neq 0$$

$$I(\omega) = \int \frac{d^3 q C(0, q)^2}{(\omega - \omega(q))^2 + \left(\frac{\Gamma_0}{2}\right)^2}$$

Raman feature of NMs predicated by MCM



Frequency and line shape of Raman spectra related with sizes!

(III) Prediction for the Raman features of nano-materials based on above models

Appearing of new Raman modes

- (1) Active mode in bulks "split" into many sub-modes such as optical mode in superlattices
- (2) Forbidden modes in bulks (e.g., acoustic modes) become active modes .
- (3) Induce new modes, e.g, the interface and surface modes.

Appearing new characteristic of active modes in bulks

- (4) Frequency shift ;
- (5) Linewidth broaden
- (6) Symmetrical Lineshape may become into unsymmetrical ones.

II-3 Observed Raman Spectra

- Examination of above predictions of Raman features

(I) Superlattices (SLs)

GaAs_{5.4nm} / AlAs_{1.8nm} Superlattices

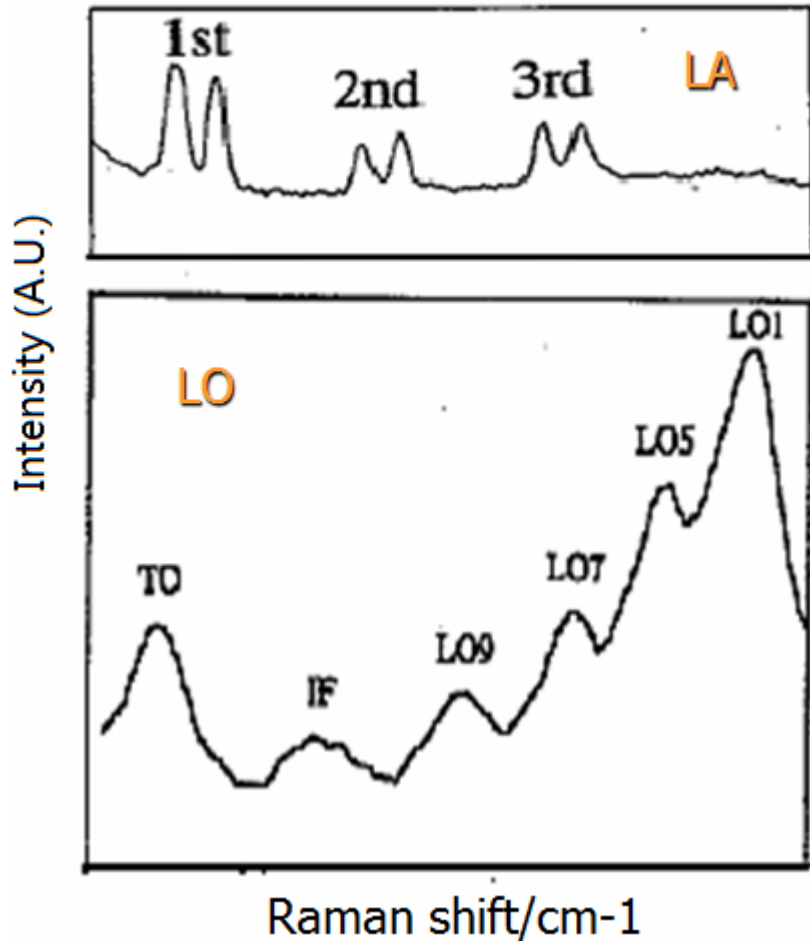
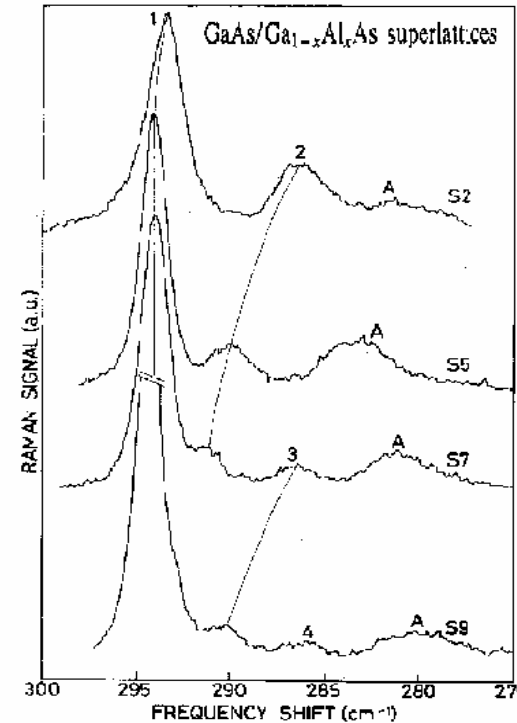


TABLE I. Sample parameters as defined in the text. For samples S6 and S8 the parameters have been estimated from the growth conditions.

	d (Å)	\bar{x}	n_1	n_2
S2	29.2	0.123	6	4
S5	51	0.147	9	9
S7	54.4	0.141	12	7
S9	81.4	0.145	17	12



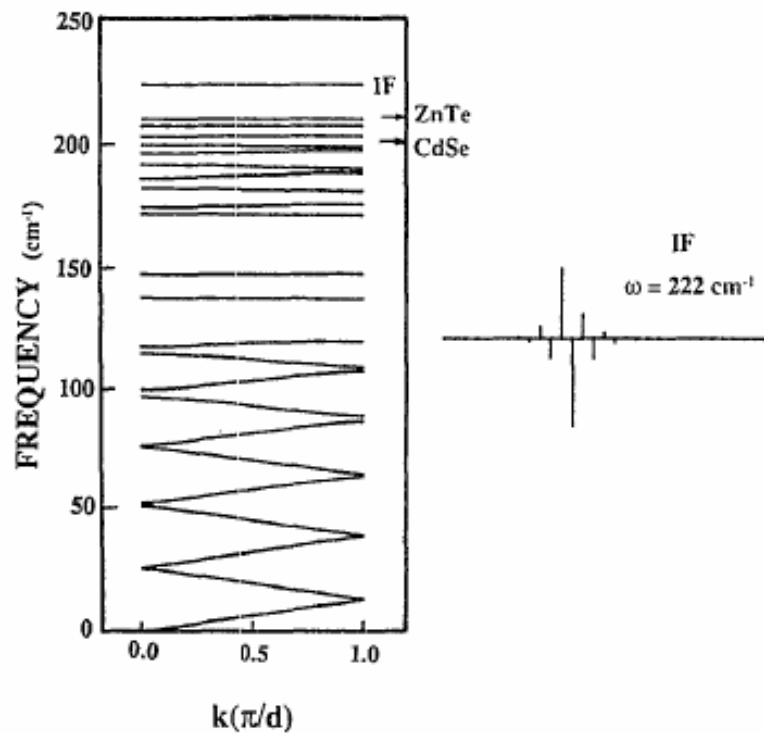
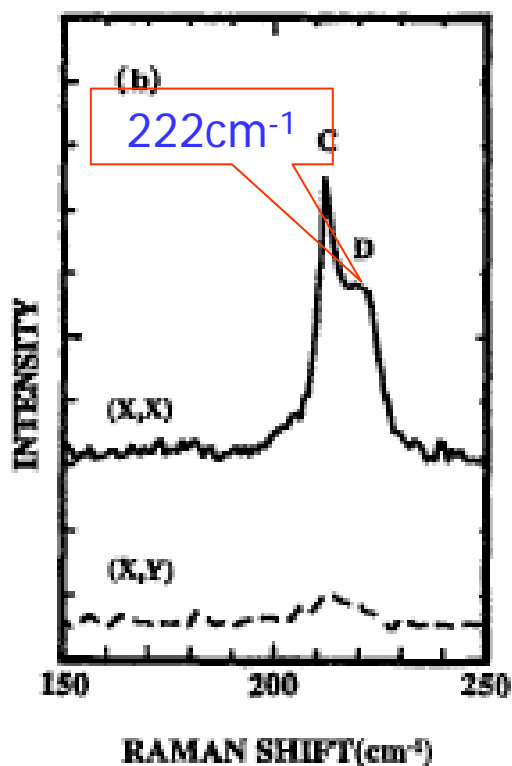
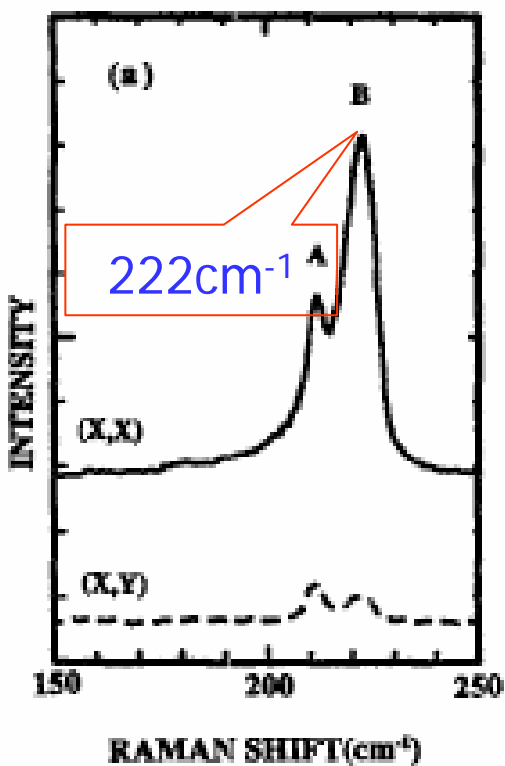
超晶格界面键的振动模
(CdSe) / (ZnTe) 的 Se-Zn键

理论比较/cm⁻¹

实验 222

Fesolino 211

我们计算 222



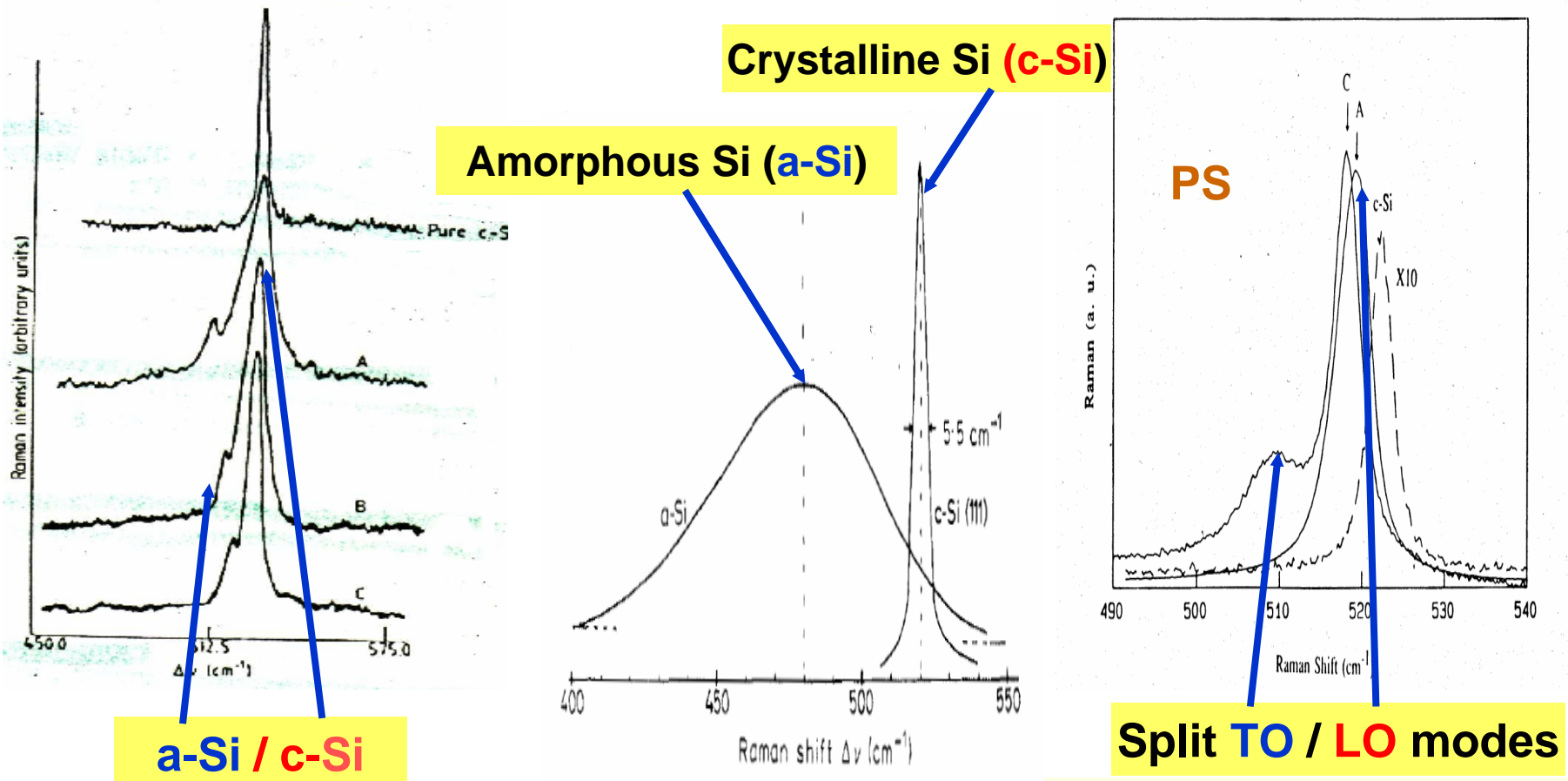
(CdSe)₄/(ZnTe)₈

(CdSe)₈/(ZnTe)₁₂

(II) Nanomaterials (NMs)

1. Porous Silicon (PS) - The first studied NMs widely

Early works: Consisted of two Bulk Raman spectra
???: Not match the prediction based FSE!



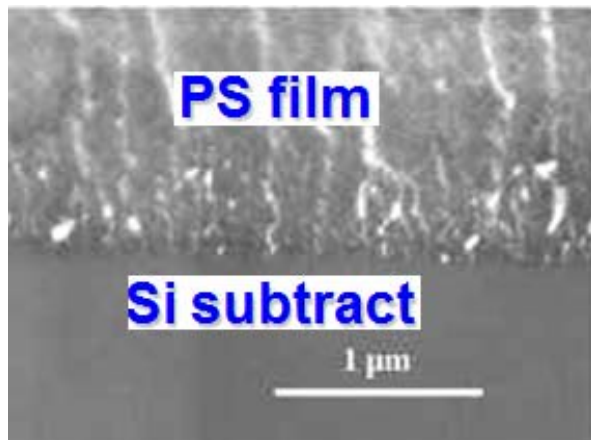
-Goods, et al, Semi. Sci. Tech. 3(1988)483

-T. Tsu, et al APL, 60(1992)112.

Analyses and measurement for PS Raman spectra

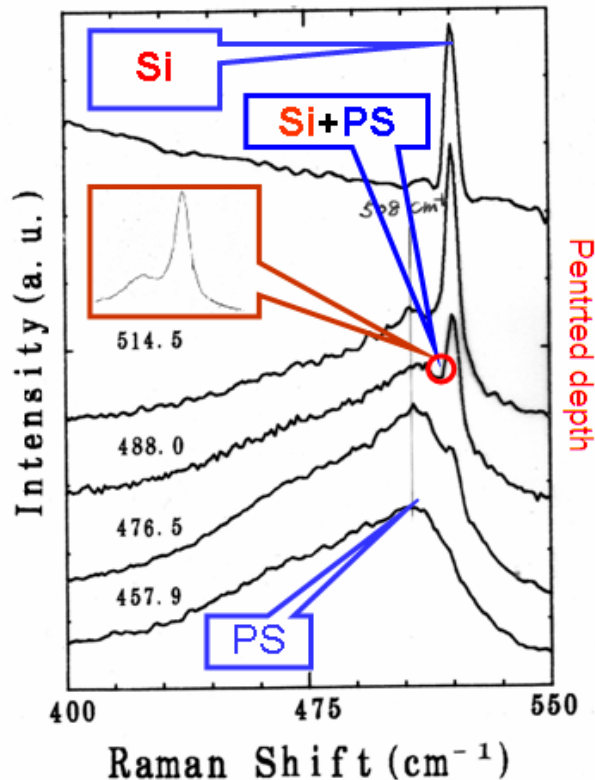
—S.L.Zhang, J. Appl Phys, 69(1995)3399; 62(1993)642

PS Structure

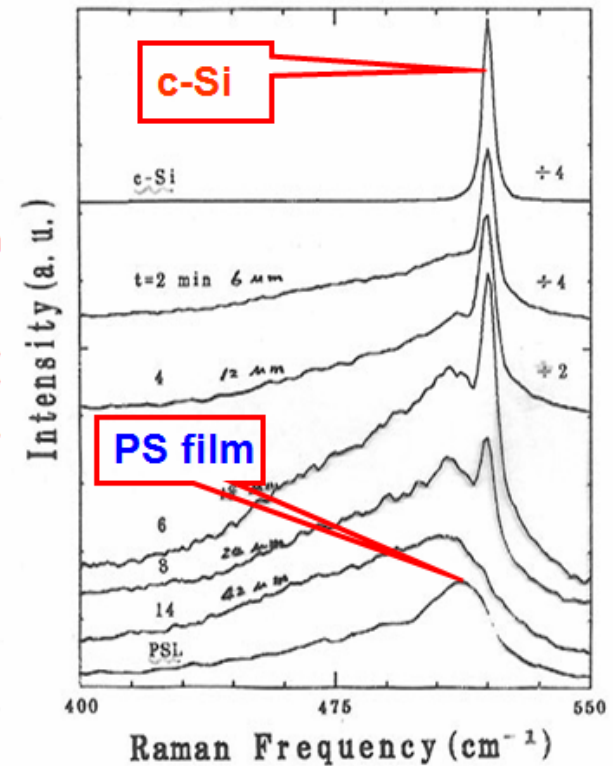


Mix two spectra of PS and Si substrate?

Change exciting light wavelength



Change PS film thickness

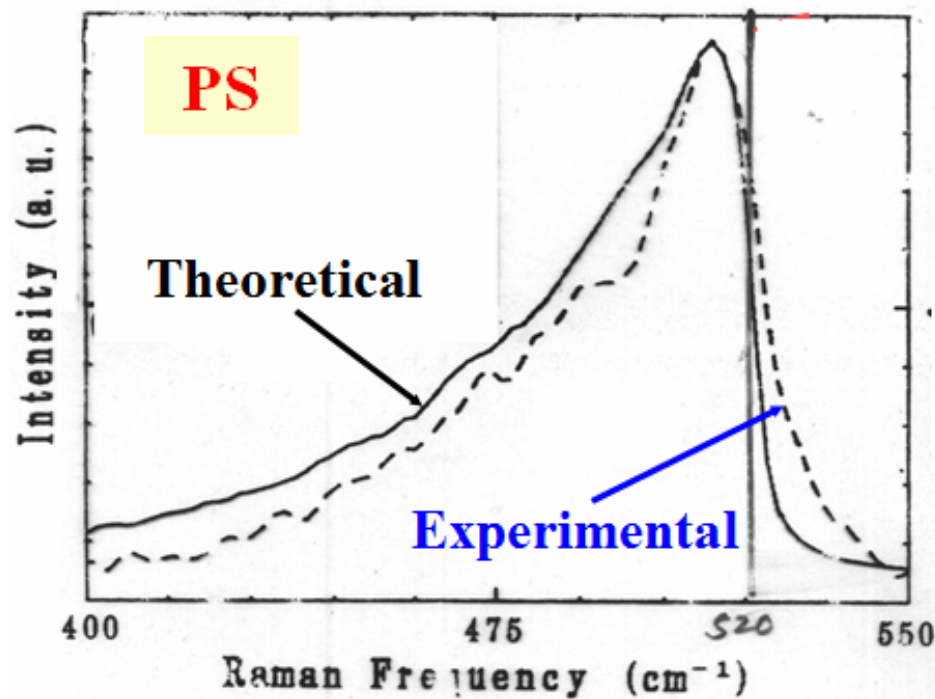


Theoretical fitting of PS Raman spectra

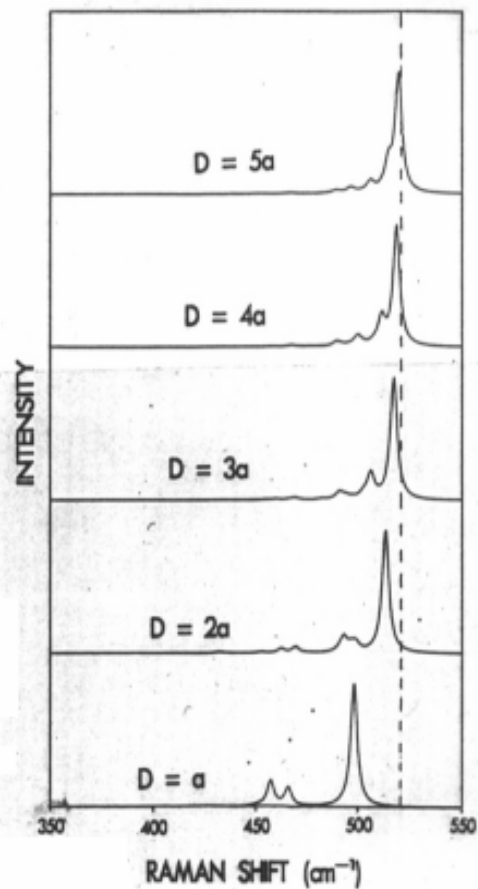
—J. Appl Phys, 69(1995)3399; 62(1993)642

(1) MCM

$$I(\omega) = \int \frac{d^3 q C(0, q)^2}{(\omega - \omega(q))^2 + (\frac{\Gamma_0}{2})^2}$$

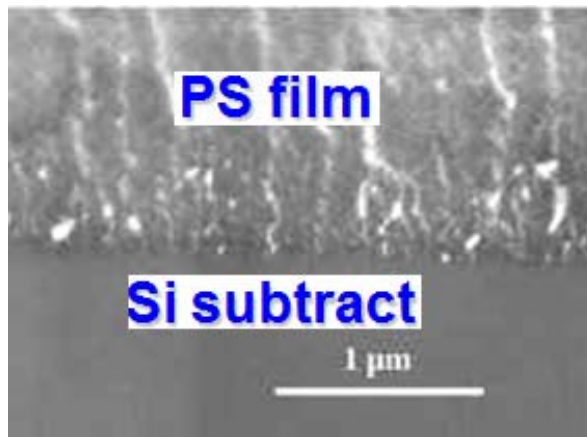


(2) Bond polarizability theory

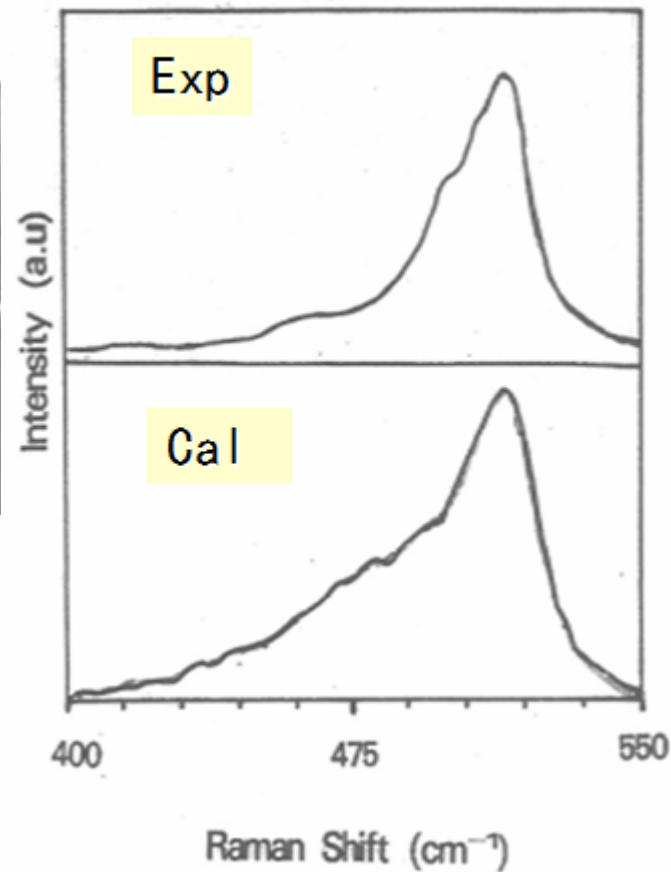


TO – LO split

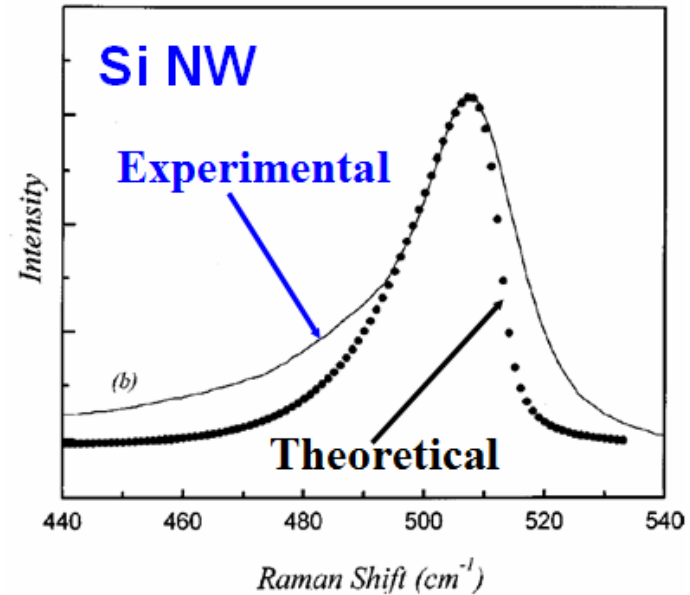
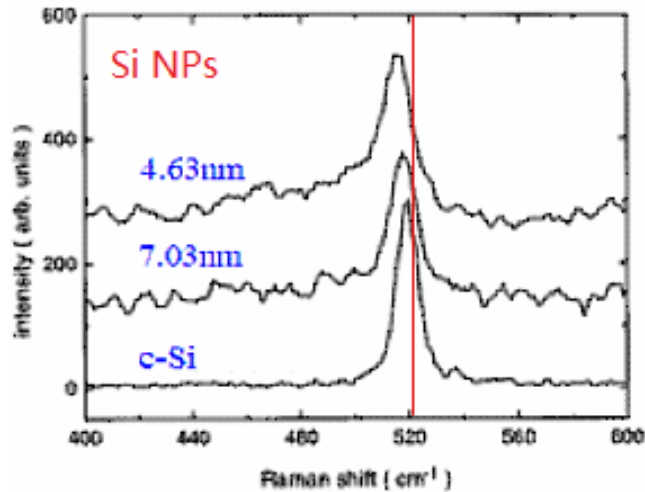
Size-distributed



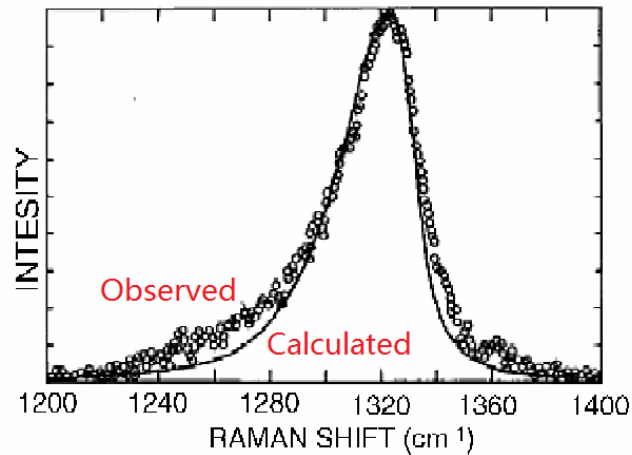
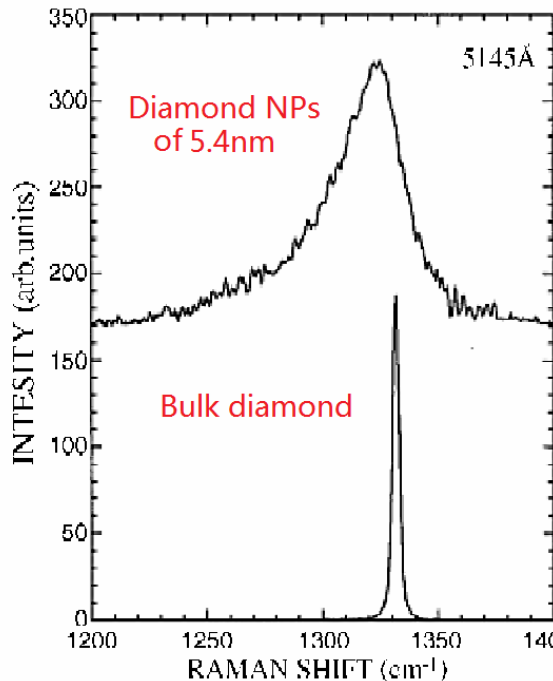
Considered size-distribution



2. Si and diamond NMs



-Ehbrecht et al. PRB,56(1997)6958



- M. Yoshikawa, et al., APL,67, 694(1995)

Brief summary

**In past 30 years
Above predication for Raman features
of nanostructured materials
was confirmed.**

**However, many novel phenomena
not fitting above predication
were also observed**

What's those ? See next chapters !

CONTENTS

I. Basic Feature of Raman Spectra and Nanostructures

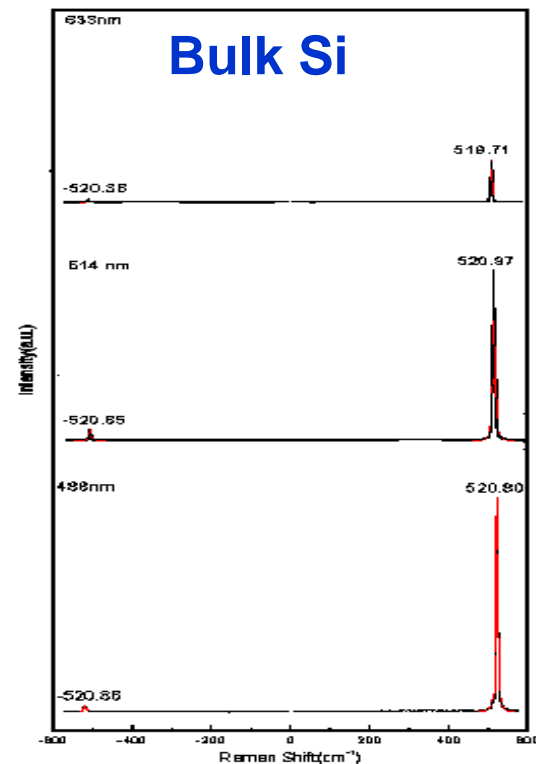
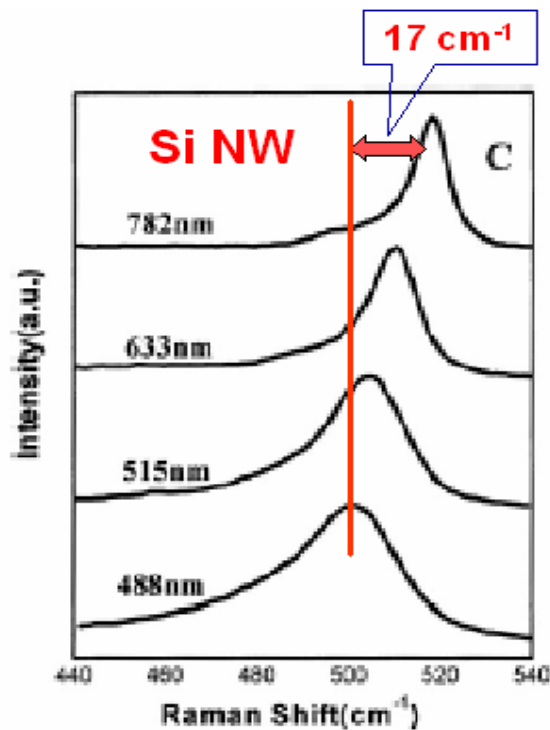
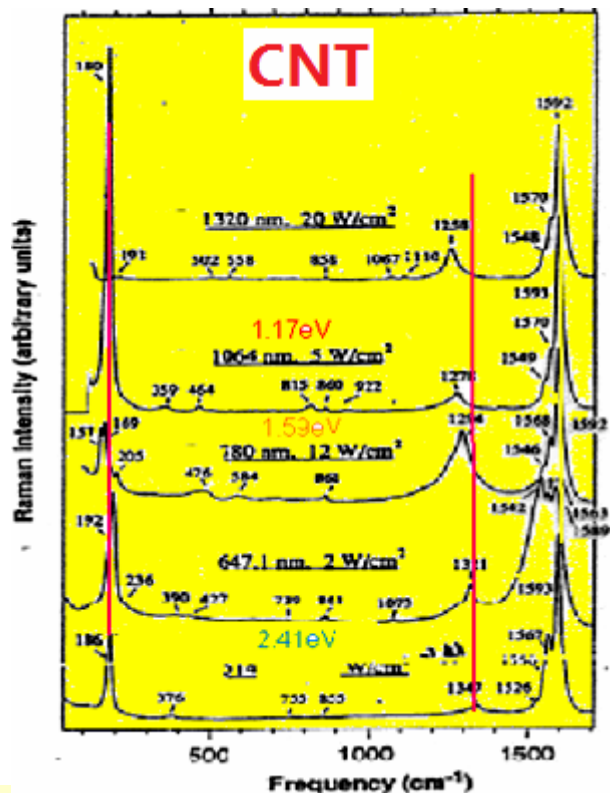
II. Raman Spectral Feature of Nano-semiconductors

III. Abnormal Raman Spectral Feature Relative to Conventional Raman Spectroscopy.

IV. Abnormal Raman Spectral Feature Relative to Nanostructure Raman Spectroscopy

III-1 Raman Frequency Dependent of Excited Wavelength-Resonant size selection effect (RSSE)

(I) Experimental results



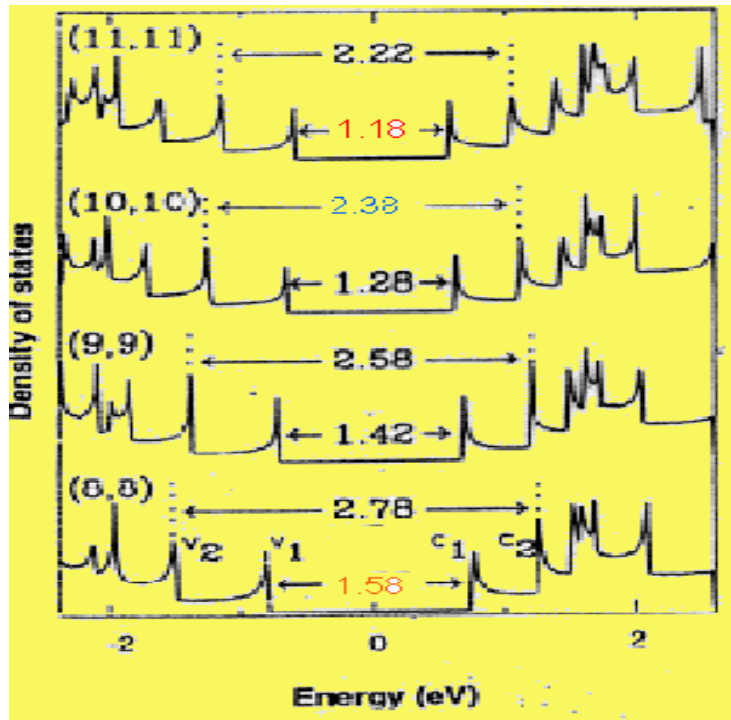
-M. Rao, et al, Science, 275, 187(1997)

Against one of universal features in traditional Raman spectroscopy: frequency independent of incident wavelength, also energy conservation law.

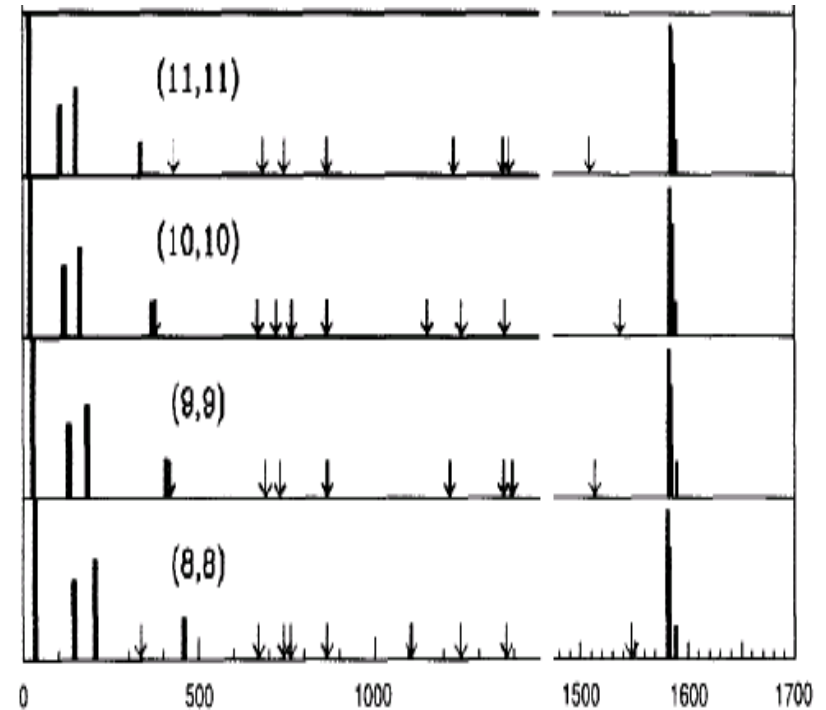
(II) Origin and nature

- Theoretical analyses - M. Rao, et al, Science, 275, 187(1997)

Calculated DOS of electron



Calculated Raman frequency



It is due to

1. Resonant Raman scattering.
2. Size-distributed NMs.

Called as resonant size selection effect (RSSE).

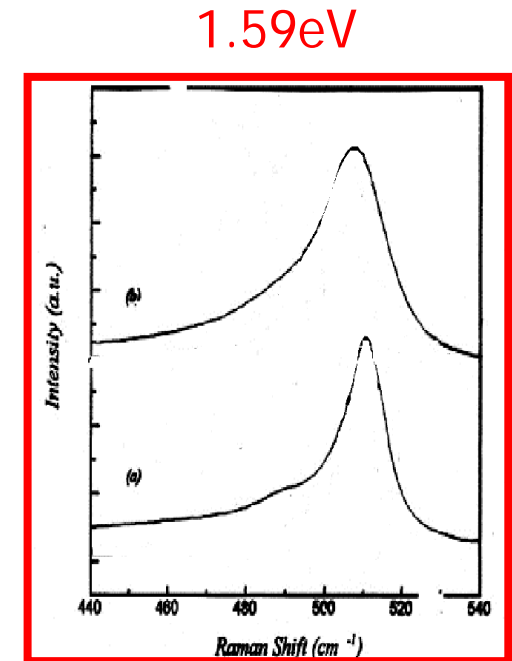
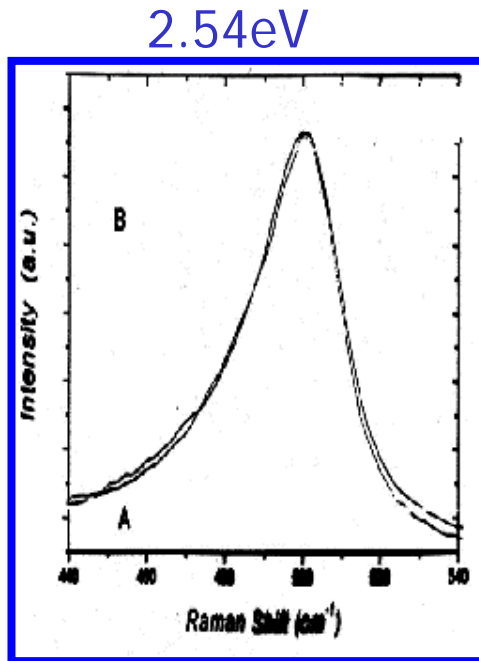
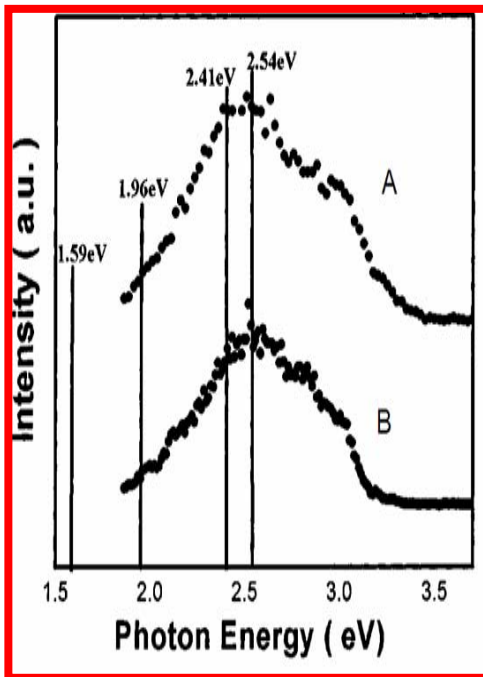
Experiment Confirmation of RSSE.

-Zhang et al, APL, 81, 4446(2002).

Different size-distributed samples

Resonance with same excited λ

Non-resonance with same excited λ



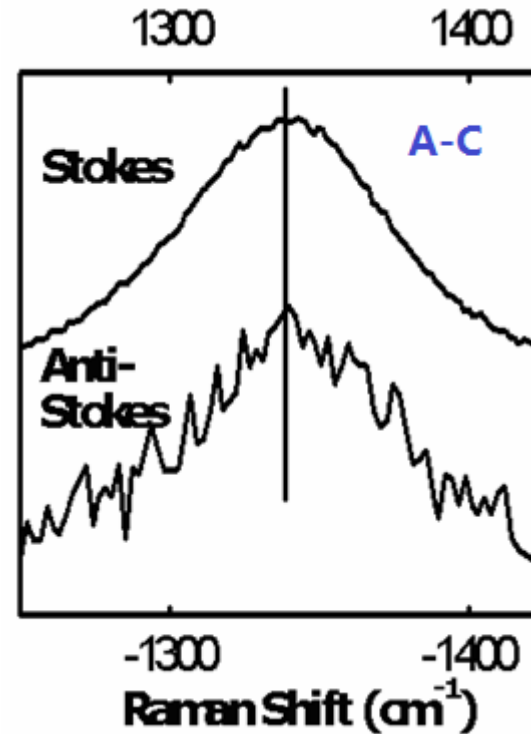
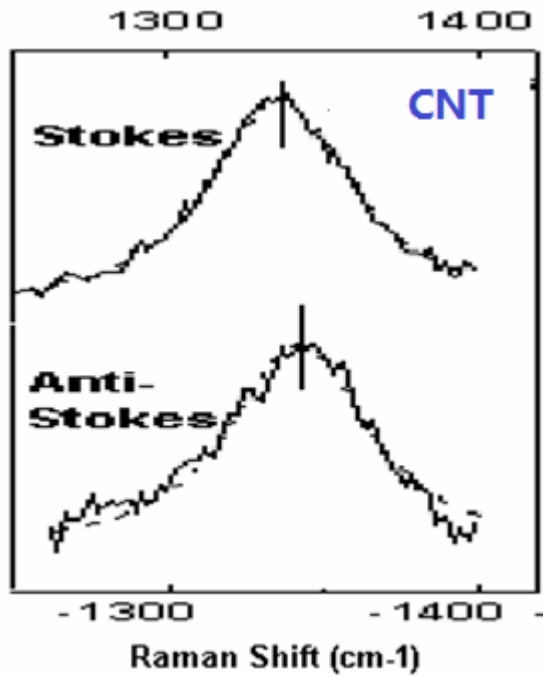
RSSE is still the FSE behavior, No violation for:

- FSE on frequency;
- Energy conservation law.

III-2 Unequal Absolute Raman Frequency of Anti-Stokes and Stokes Peaks

-Phys Rev B, 66(2002)05431

(I) Experimental results



In CNTs, found $\Delta = |\omega_{AS}| - |\omega_S| \neq 0$
Against to universal feature two.

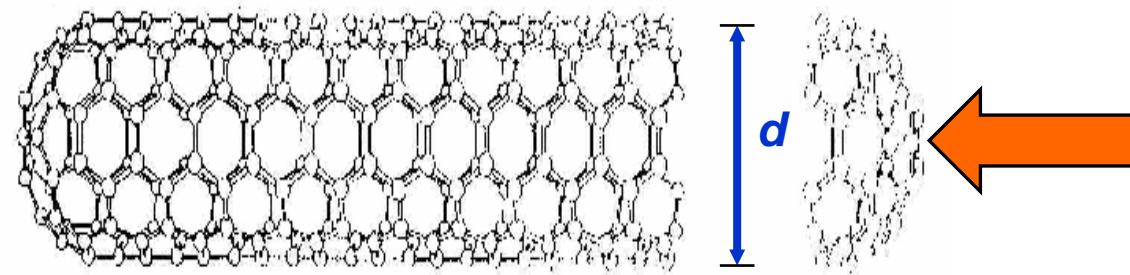
(II) Origin and nature of $\Delta \neq 0$

Δ values of CNTs and perfect graphite - HOPG

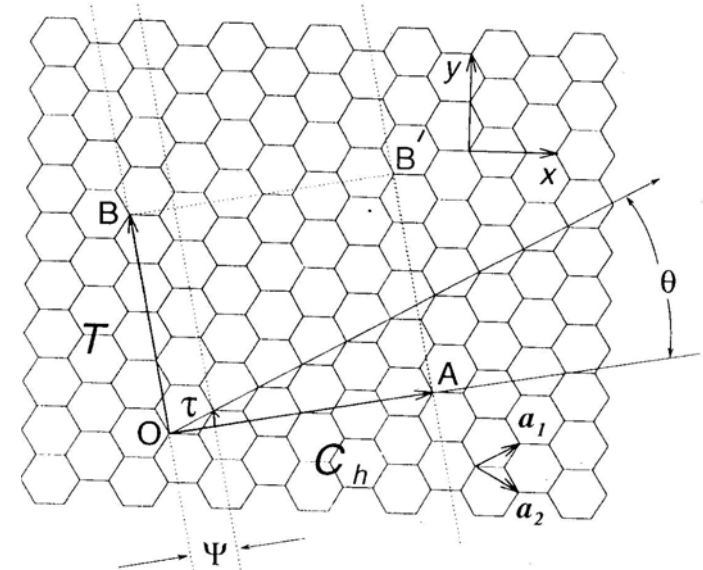
Sample	MW-CNT	SW-CNT	HOPG	HOPG _{Au}
$ \omega_{As} - \omega_s $	+7	+7	/	-7.7
Δ	$\neq 0$	$\neq 0$	= 0	$\neq 0$

- $\Delta \neq 0$ Related with tubular structures !
- $\Delta \neq 0$ Related with defected materials !

Inspect CNT structure:



Graphite tube

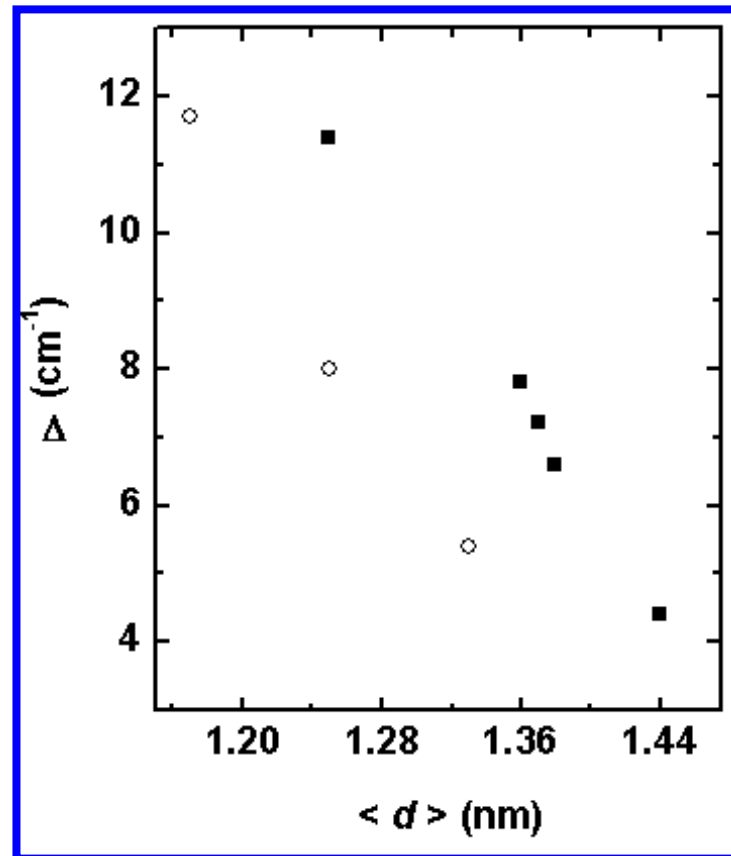


**Graphite sheet-
HOPG**

1. CNTs is a **defect** structure; Defects $\sim d$.
2. $\Delta \neq 0$ may **from tubular structure itself!**

Expectation:
Larger the $\langle d \rangle$, Smaller the Δ

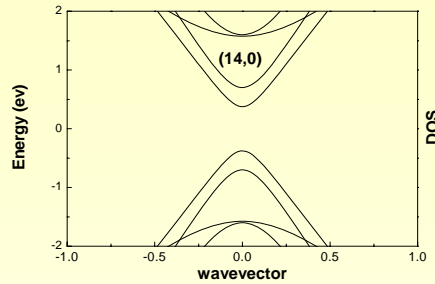
● **Experimental confirmation**



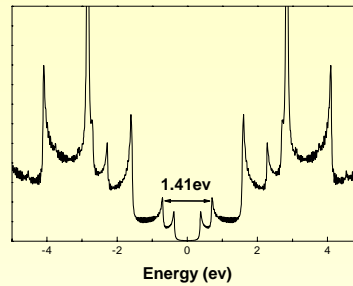
Confirmed experimentally

● Theoretical calculation

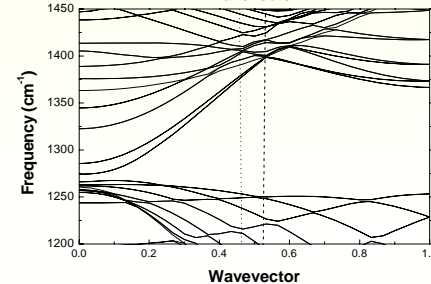
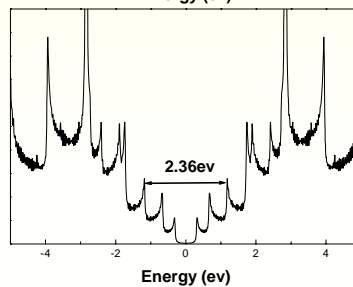
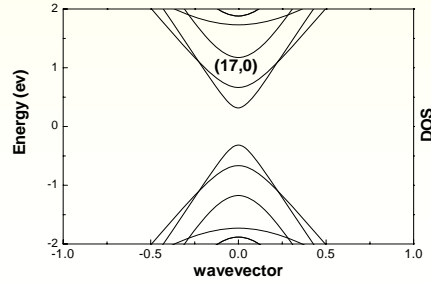
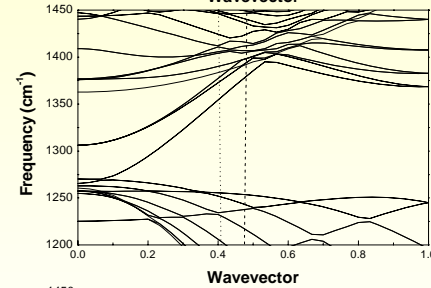
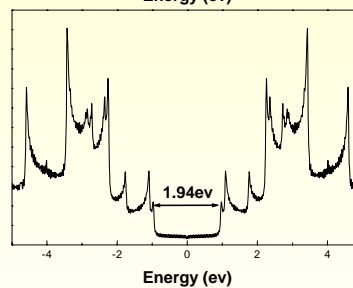
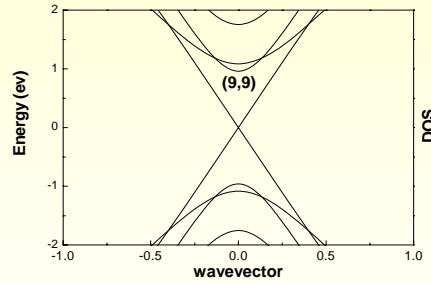
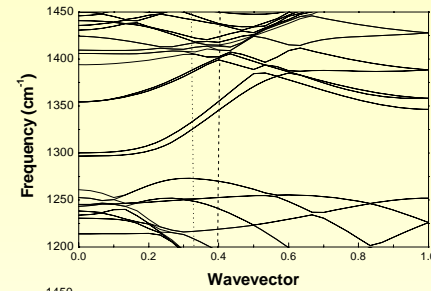
Energy band



DOS



Phonon dispersion



Found

Double resonance can be happened in CNTs

Calculate Δ by double resonance

$$q = (E_I - h\omega_{ph}) / \nu_1 \text{ or } (E_I - h\omega_{ph}) / \nu_2 \quad (1)$$

$$\omega_{ph}(q) = f(q) \quad (2)$$

Comparison between observation and calculation

Tube	ω_S (cm ⁻¹)	ω_{AS} (cm ⁻¹)	Error(%)	Δ (cm ⁻¹)
(17,0) Cal.	1388	-1349	4	+6
Obs	1337	-1342		+5
(9, 9) Cal	1399	-1408	6	+9
Obs	1314	-1322		+8

Confirmed theoretically

Brief summary

- The **RSSE** is an embody of **FSE**, i.e.,:

$$\text{RSSE} \approx \text{FSE}$$

- The $|\omega_{As}| - |\omega_s| \neq 0$ explores a important nature of nanostructures.

● Above two 'abnormal' are originated from the defect property of sample: intrinsic and artificial defects, respectively.

● Therefore It is should be expected from bulk/traditional Raman spectroscopy and the principle of Raman scattering and two basic laws are still hold in nanostructures.

CONTENTS

I. Basic Feature of Raman Spectra and Nanostructures

II. Raman Spectral Feature of Nano-semiconductors

III. Abnormal Raman Spectral Feature Relative to Conventional Raman Spectroscopy.

IV. Abnormal Raman Spectral Feature Relative to Nanostructure Raman Spectroscopy

IV-1 Abnormal Feature of Raman Frequency

APPLIED PHYSICS LETTERS

VOLUME 81, NUMBER 23

2 DECEMBER 2002

Variation of Raman feature on excitation wavelength in silicon nanowires

Shu-Lin Zhang,^{a)} Wei Ding, Yan Yan, Jiang Qu, Bibo Li, Le-yu Li, Kwok To Yue,

e.g., SiC nanorods,^y consisting of smaller grains, we expect that a similar Raman scattering should be present in such kinds of systems.

It is reasonable, but not observed!

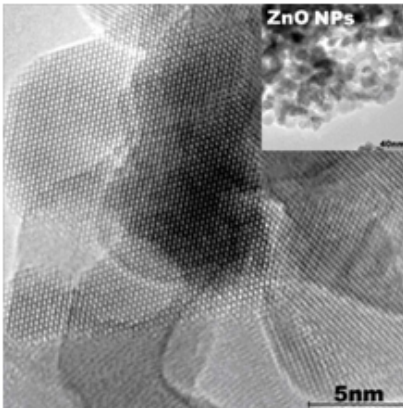
A. Frequency Feature

A-1. No RSSE

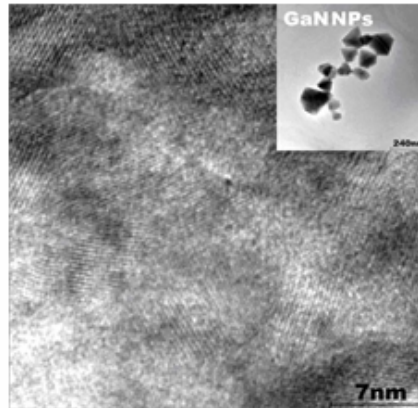
(I) Sample

HRTEM

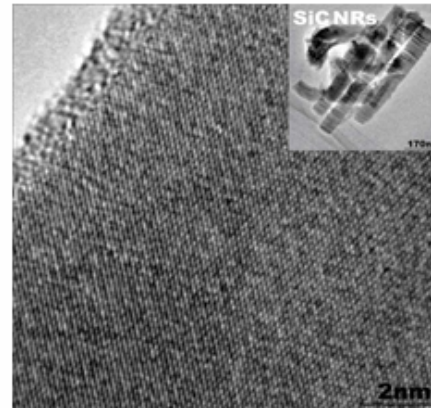
ZnO NPs



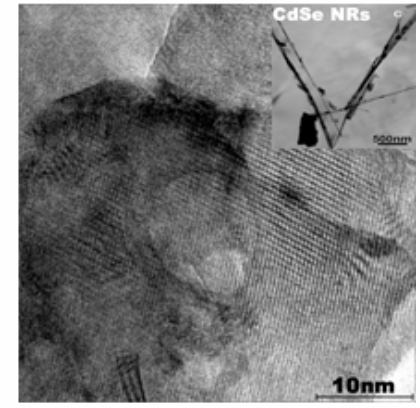
GaN NPs



SiC NRs



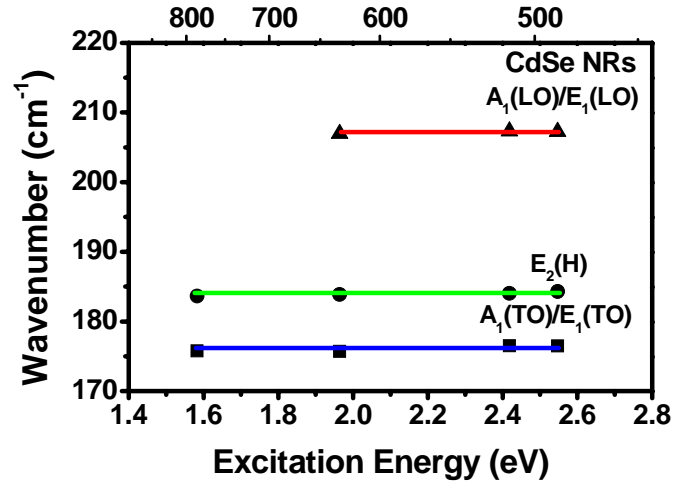
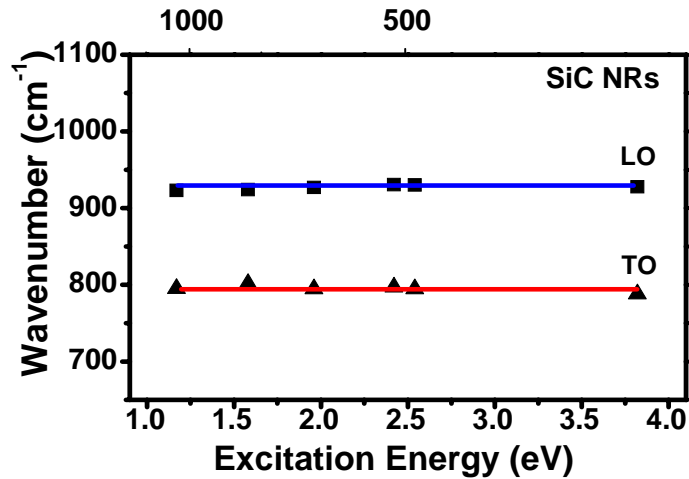
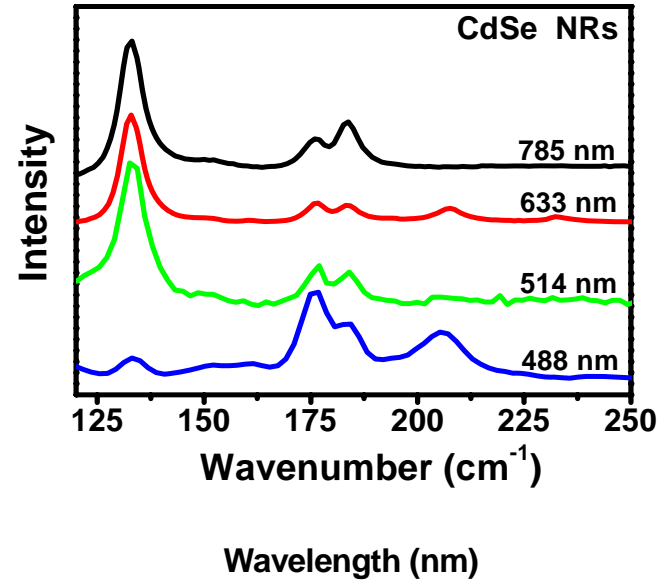
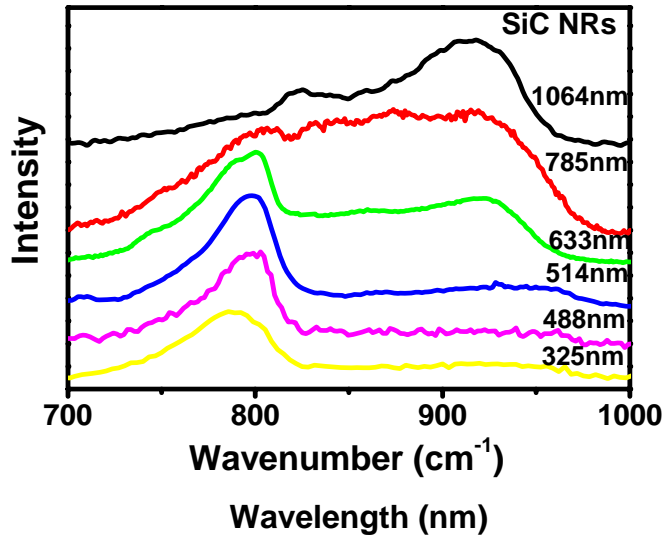
CdSe NRs

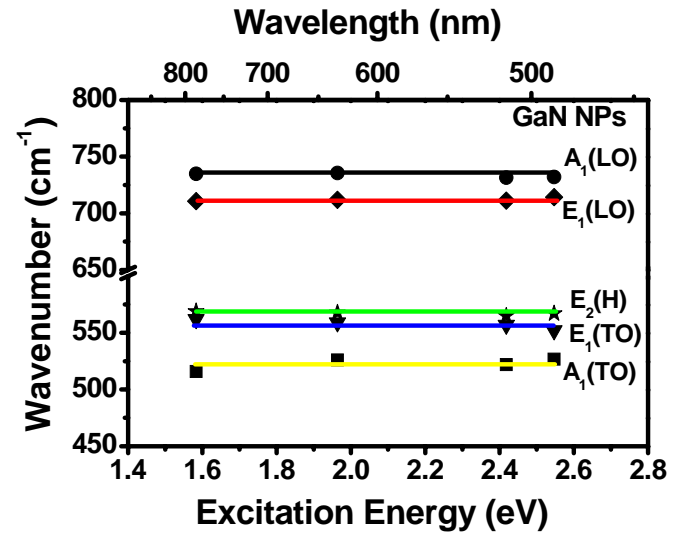
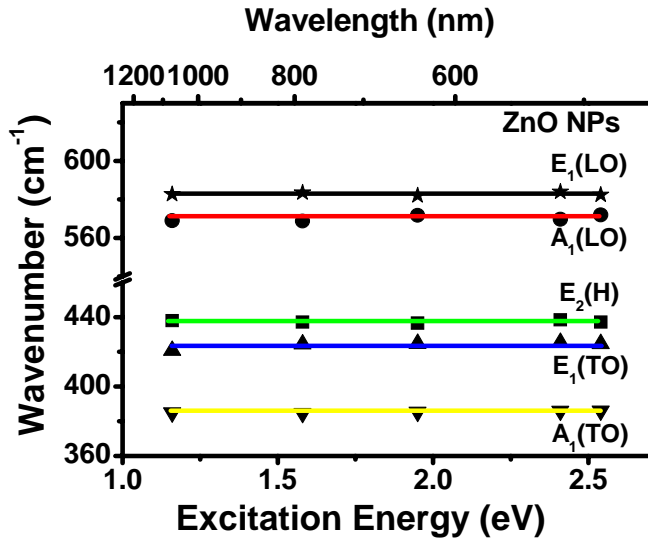
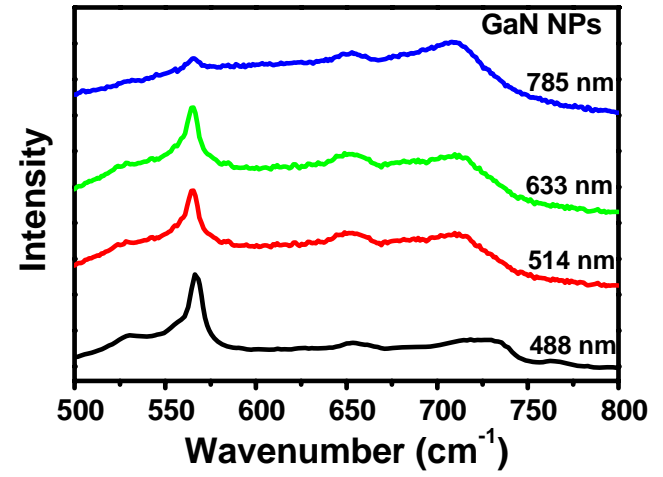
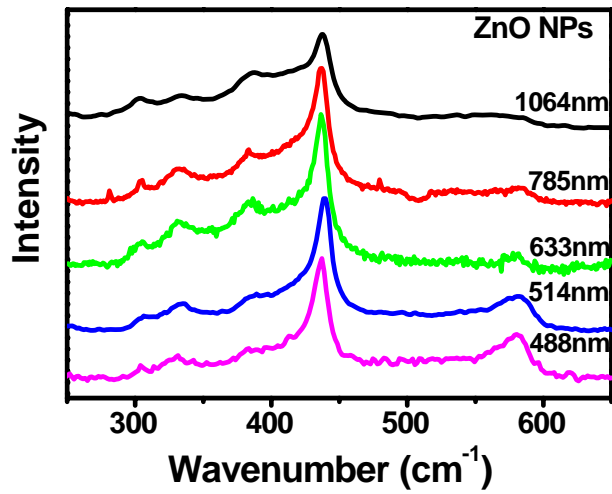


The samples are consisted of
a collection of crystalline grain with different sizes

Sample	ZnO NPs	GaN NPs	SiC NRs	CdSe NRs
$L_{Average}$	7nm	4nm	10nm	4nm

(II) Observed result



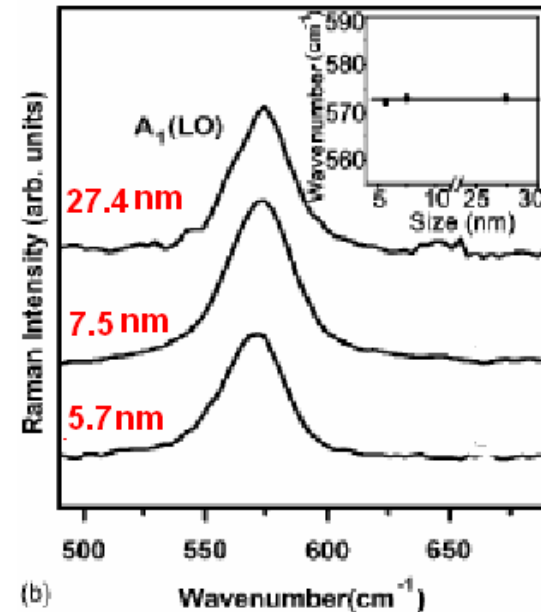
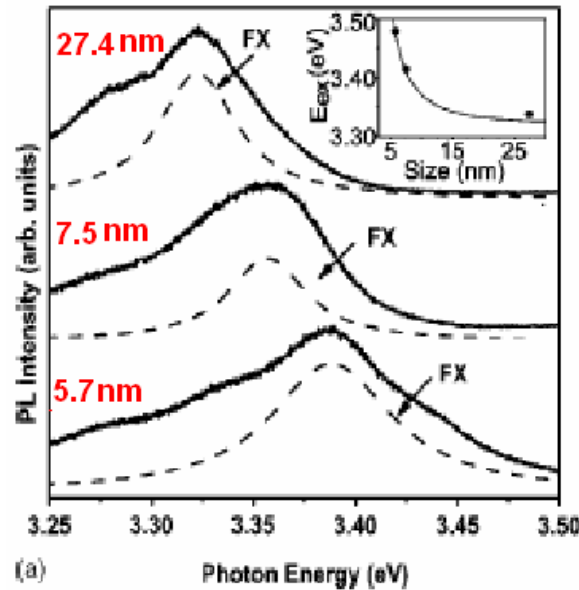


RSSE is not found!

(III) Origin and nature

Suggested Origin 1 : Sample sizes not too small to induce FSE

Test : by PL /Raman spectra for same group ZnO NPs
 - Z. D. Fu, et al, Appl Phys Lett., **90**, 263113(2007).

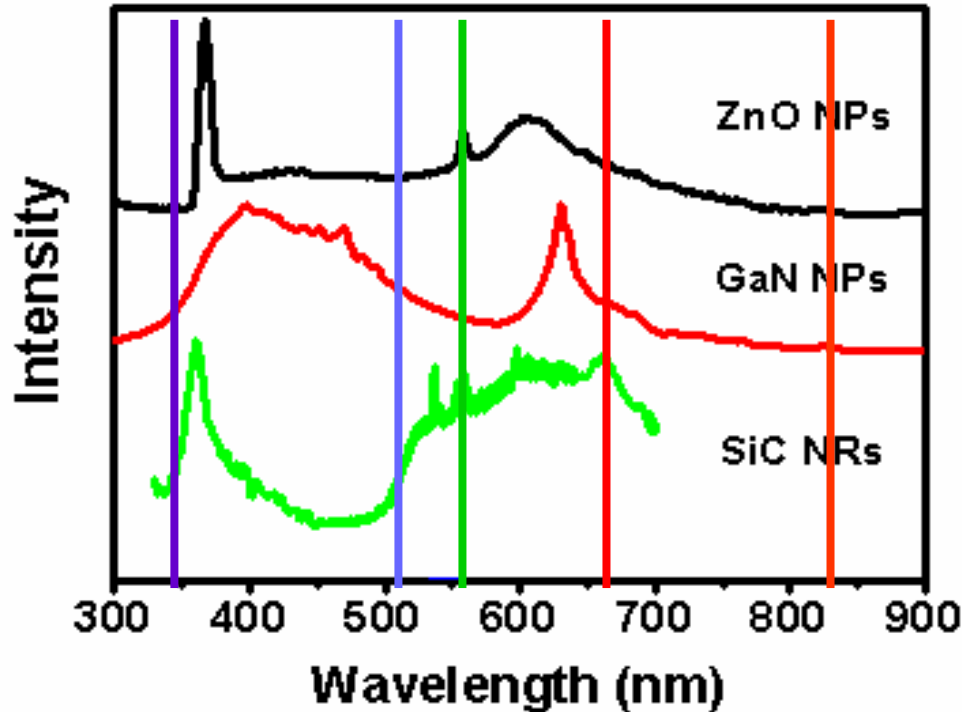


Size (nm)	5.7	7.5	27.4
EXP	3.388	3.355	3.313
THEO	3.389	3.357	3.319

FSE? PL: Yes! Raman: No!

Suggested Origin 2 : Not in resonance

-S.L.Zhang et al, APL, **89**, 063112(2006):



Electron transition energy cover a broad wavelength region.



is

resonant Raman spectra

**Meet conditions: 1. Size-distributed NMs;
2. Resonant Raman scattering.
Should expect the RSSE. But no!**

Suggested Origin 3 : Resonance with impurities/defects

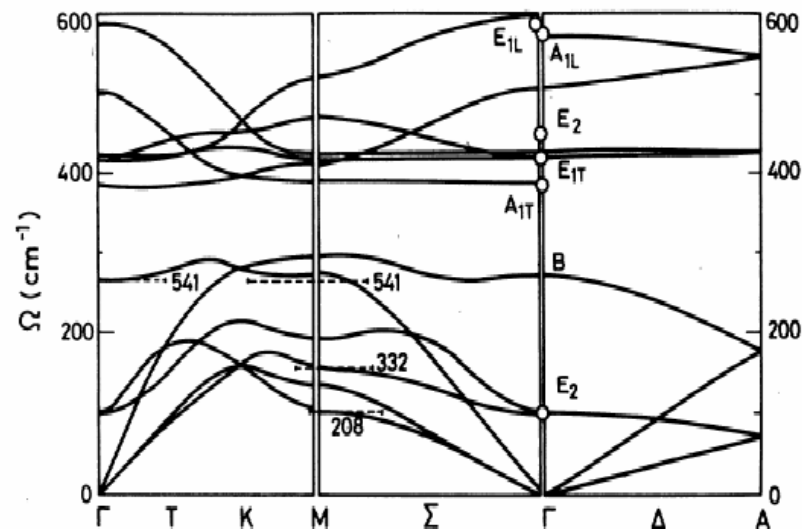
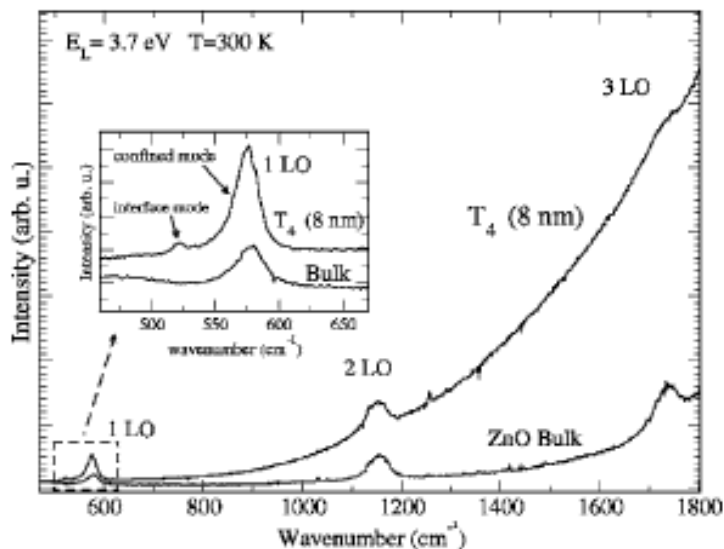
As the condition of such kind of resonance:
The energy of exciting light must be below E_g .

Check:

Sample	E_g (eV)	E of laser (nm/eV)					
		1054 /1.18	785 /1.58	633 /1.96	514 /2.41	488 /2.54	325 /3.82
ZnO	3.2	✓	✓	✓	✓	✓	✗
GaN	3.44	✓	✓	✓	✓	✓	✗
CdSe	1.8	✓	✓	✗	✗	✗	✗
SiC	2.4	✓	✓	✓	✗	✗	✗

✗: High than E_g . **Not all are in gap!**

Suggested origin 4: No much or not ispersive



-F. Demangeot *et al.*, Appl. Phys. Lett. 88 (2006)071921.

size. This seems however understandable looking at the optical phonon dispersion curves which are very flat near the Brillouin zone center. However, further work needs to be

See the deviated values

at 1/4 away from the center of Brillouin zone

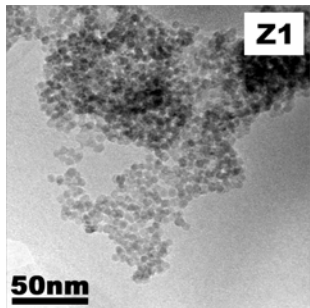
Phonon		ZnO		GaN	CdSe	3C-SiC
E_{1L}	LO	8.7	/	0	1.3	33.3
A_{1T}		1.3	/			
A_{1L}		/	1.3	2.4	1.3	
$E_2(H)$		/	0	1.2	0.3	
E_{1T}		/	0			
$E_2(L)$	TO	/	2.5	2.4	0.3	8.3
		$\Gamma-\Sigma$	$\Gamma-A$			

Red numbers: Much dispersive values.
Not all are little dispersive

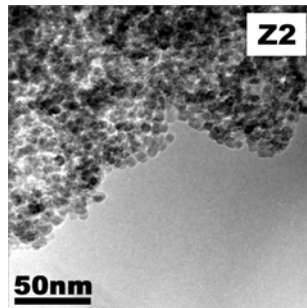
A-2. No FSE

- Appl Phys Lett, **89**, 243108 (2006,

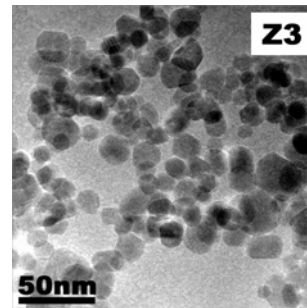
(I) Sample: Nearly Uniformed **ZnO NPs** samples



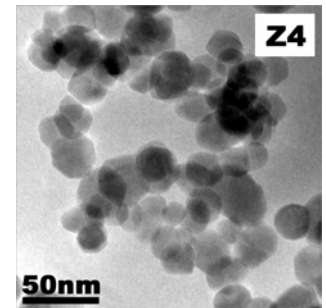
$5.7 \pm 0.6 \text{ nm}$



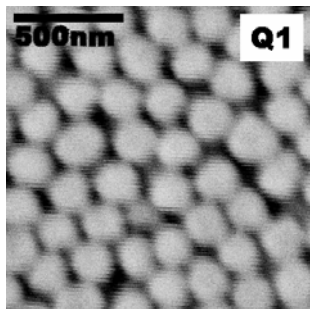
$7.5 \pm 0.9 \text{ nm}$



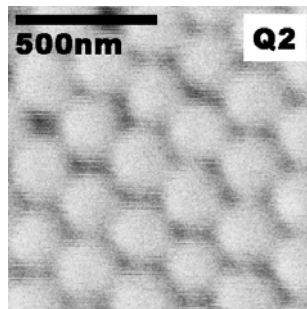
$18.2 \pm 1.7 \text{ nm}$



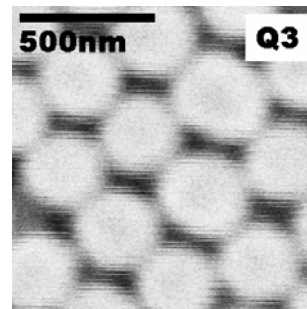
$27.4 \pm 1.8 \text{ nm}$



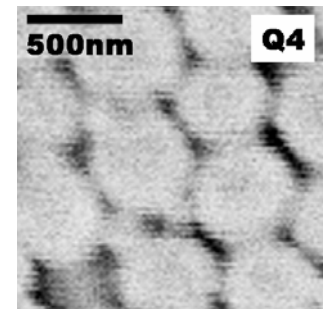
$170 \pm 10 \text{ nm}$



$250 \pm 10 \text{ nm}$



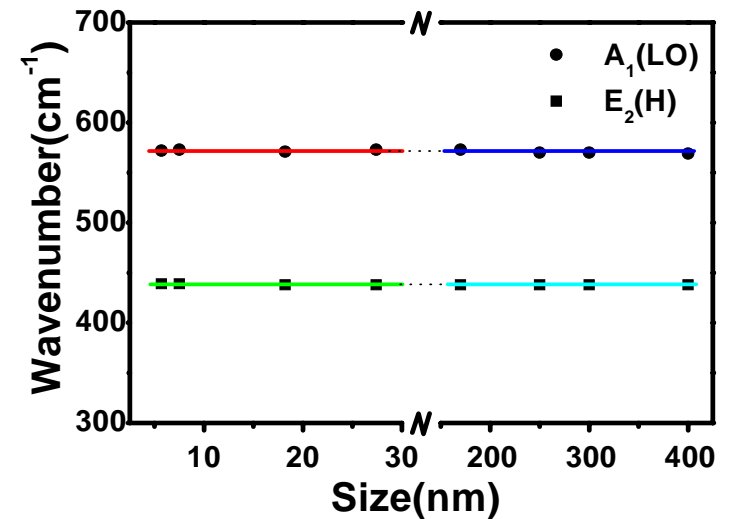
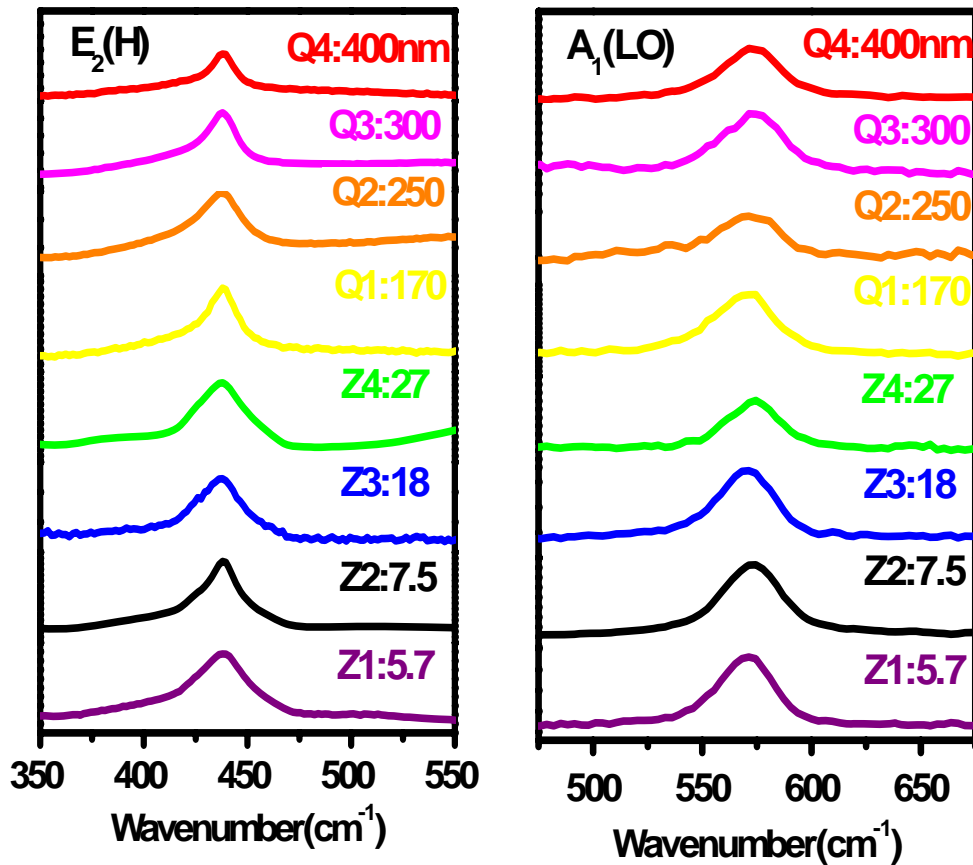
$300 \pm 9 \text{ nm}$



$400 \pm 12 \text{ nm}$

Size deviation $\leq 10\%$ ~ Nearly Uniformed!

(II) Single-phonon Raman spectra of $E_2(H)$ and $A_1(LO)$ modes

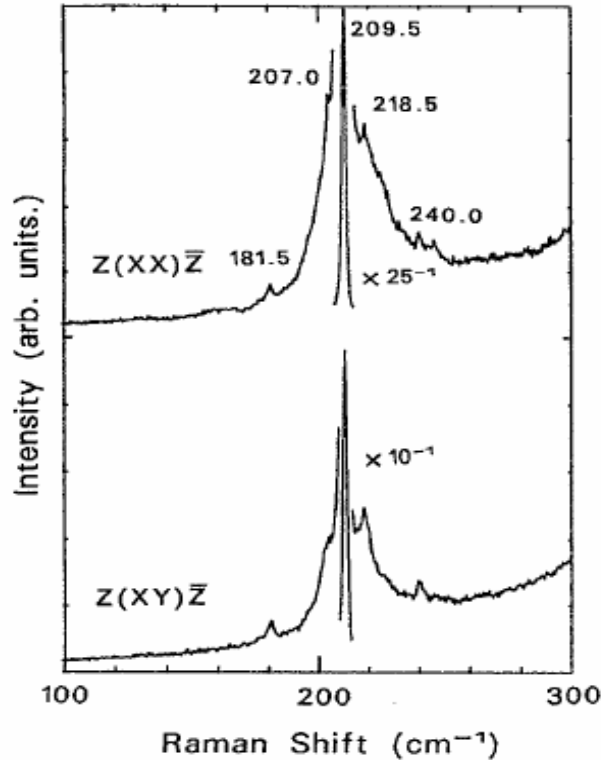


The Raman frequency not change with sample sizes

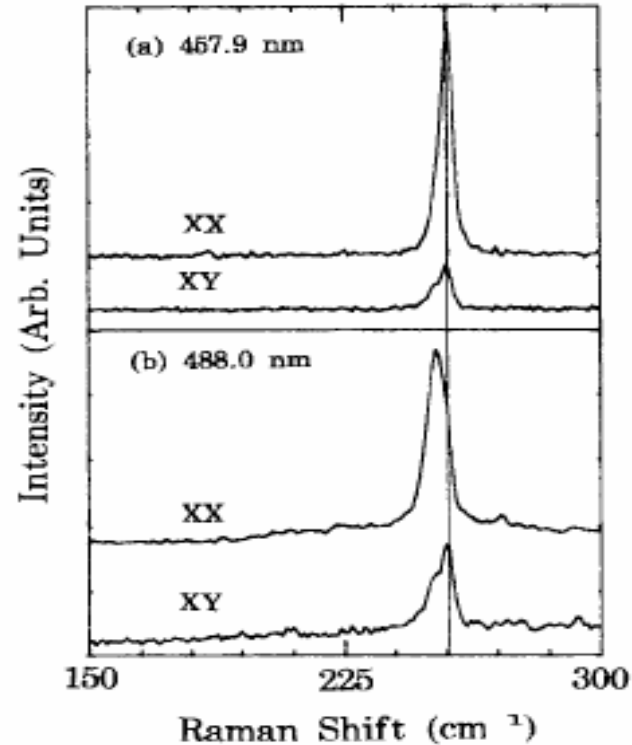
B. Selection Rule

B-1 LO modes

- (CdTe)₂(ZnTe)₄/ZnTe MQWs
– PRB,47 (1993)12937



- [(CdSe)₁(ZnSe)₃]₁/(ZnSe)₁₃₀ MQWs
– Phys Lett A, 186(1994)433



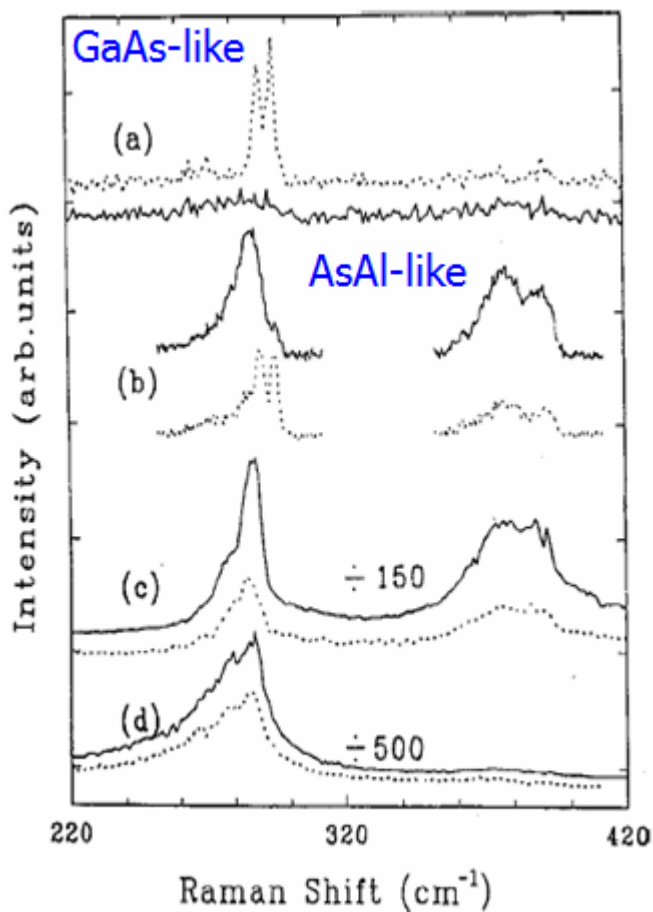
Selection rule of LO

Experimental	XY	XX
Theoretical	XY	/

B-2 Interface (IF) Modes of $(\text{GaAs})_4/(\text{AsAl})_2$ SLs

(I) Experimental results

-JAP. 76(2000)2053



	GaAs-like				AlAs-like			
	Low F		High F		Low F		High F	
	XY	XX	XY	XX	XY	XX	XY	XX
Theo_{Huang}	○		○		○	○	○	○
Exp	○	○	○	○	○	○	○	○

The result is not matching the selection rule by Huang and Zhu. The model is incorrect?

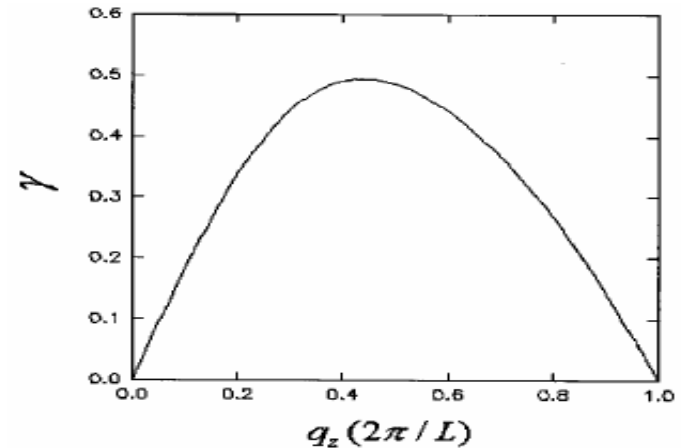
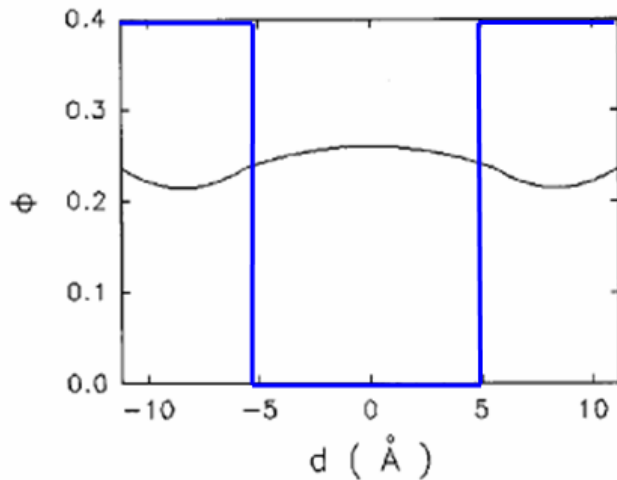
(II) Origin

Huang-Zhu model has two precondition:

1. Electronic wave-function Φ is confined in QWs.
2. Parity γ is definite.

The origin may be the sample not match the preconditions.

Calculated Φ and γ of the sample



- Electron is not confined and retransmitted (bulk-like);
- Parity is not definite.

The suggested origin is conformed and also give the correctness of H-Z model a new conformation.

C. Spectral ensemble Features

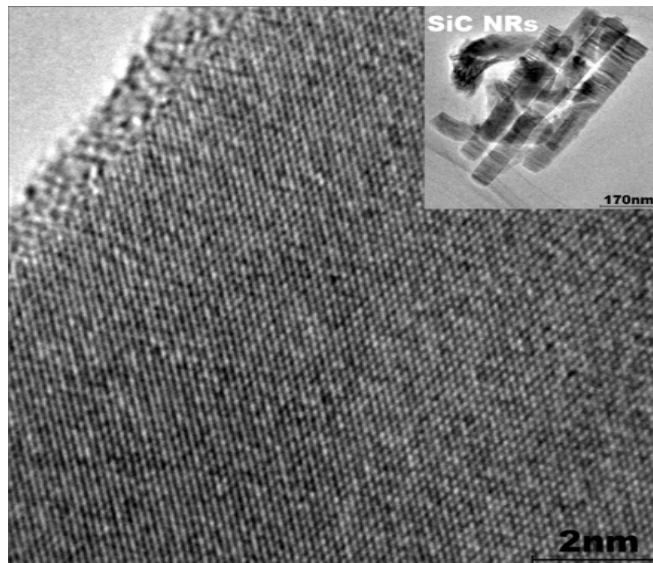
C-1 Single Phonon

- Solid State Commu. 111(1999) 47.

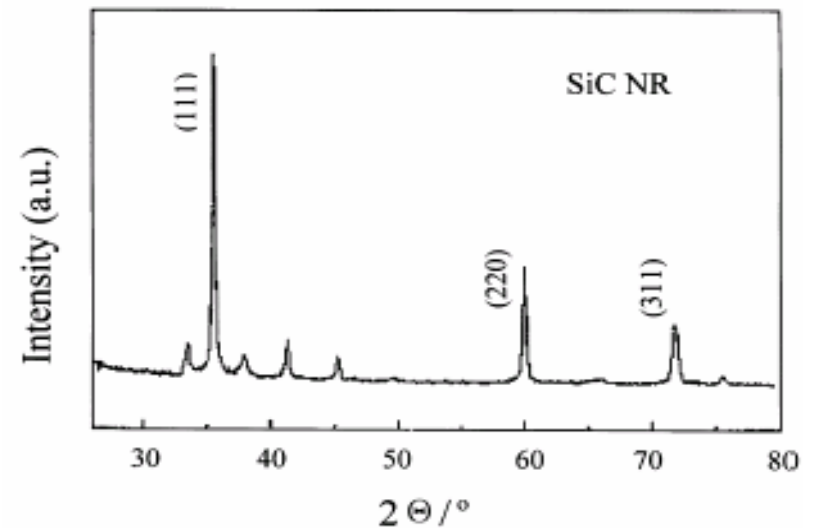
(I) Sample

Crystalline SiC Nano-roads (NRs)

Morphology /TEM



Structure/X-ray diffraction

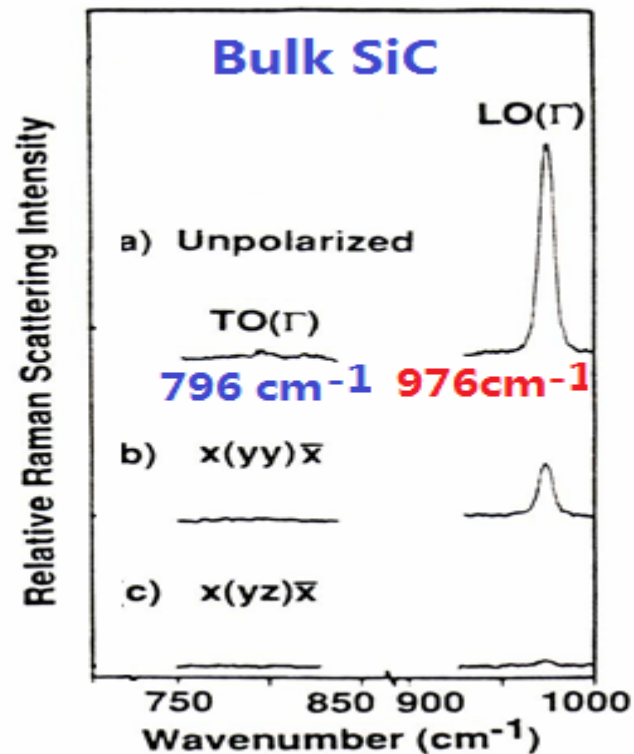
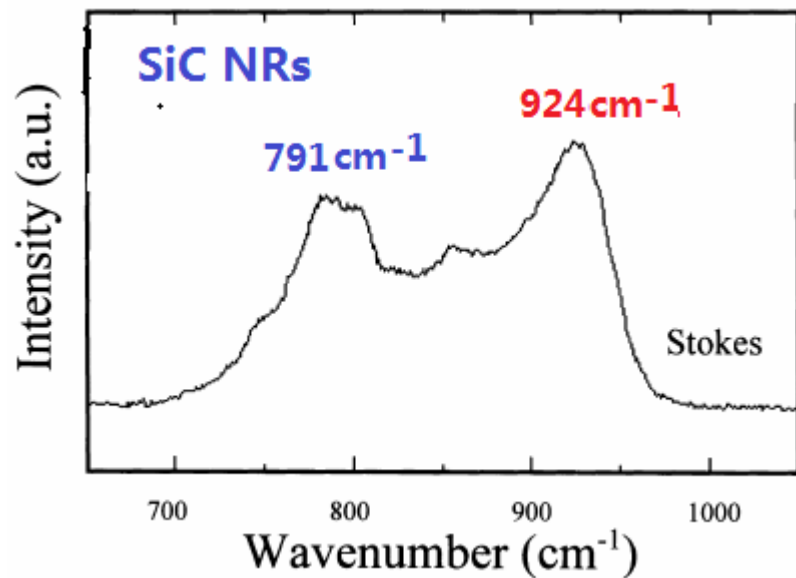


Diameters range from 3-30 nm

Zincblende nano-crystal (β -SiC).

(II) Raman spectrum

1. Observed result



— Z. C. Feng et al, JAP, 64(1988)3176.

Should be identified !

2. Identification by theoretical result

In nano-semiconductors, crystalline and amorphous Raman spectra can be fitted, respectively, by

Micro-crystal model (MCM)

$$I(\omega) = \int \frac{d^3q C(0, q)^2}{(\omega - \omega(q))^2 + \left(\frac{\Gamma_0}{2}\right)^2}$$

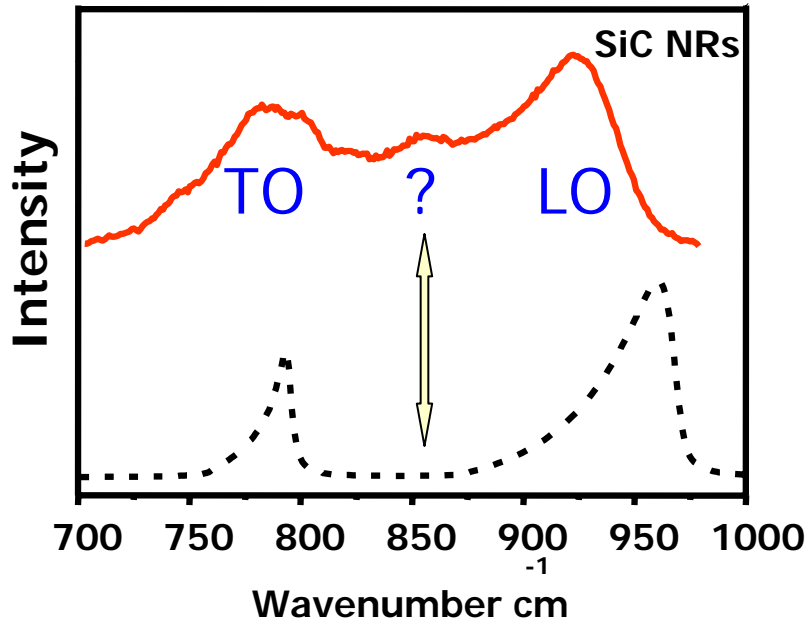
Amorphous-crystal model (ACM)

$$I_{\alpha\beta,\gamma\delta}(\omega) = \sum_b C_b \alpha\beta,\gamma\delta [(1+n(\omega))/\omega] D_b(\omega)$$

MCM and ACM fitted spectra are recognized as crystalline and amorphous, respectively.

MCM

$$I(\omega) = \int \frac{d^3q C(\mathbf{0}, q)^2}{(\omega - \omega(q))^2 + (\frac{\Gamma_0}{2})^2}$$

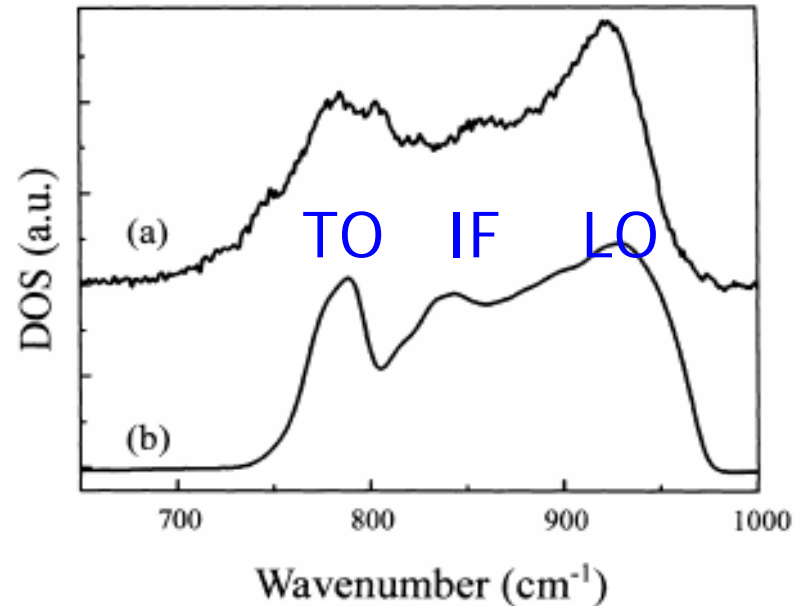


Can't fit by MCM:

LO mode: $\omega_{\text{cal}} - \omega_{\text{Exp}} = 31 \text{ cm}^{-1}$;
 No Peak at middle in calculated one.

ACM

$$I_{\alpha\beta, \gamma\delta}(\omega) = \sum_b C_b^{\alpha\beta, \gamma\delta} [(1+n(\omega))/\omega] D_b(\omega)$$



Good fitting By ACM:
 Raman spectrum of SiC
 crystalline NRs
 possesses
 amorphous feature

C-2 multiple phonons

-Phys. Rev., B52, 1477(1995).

Features of MP in traditional Raman spectroscopy:

- Frequency

$$\omega_k = k\omega_1 \sim \omega_k / k = \omega_1$$

- Linewidth

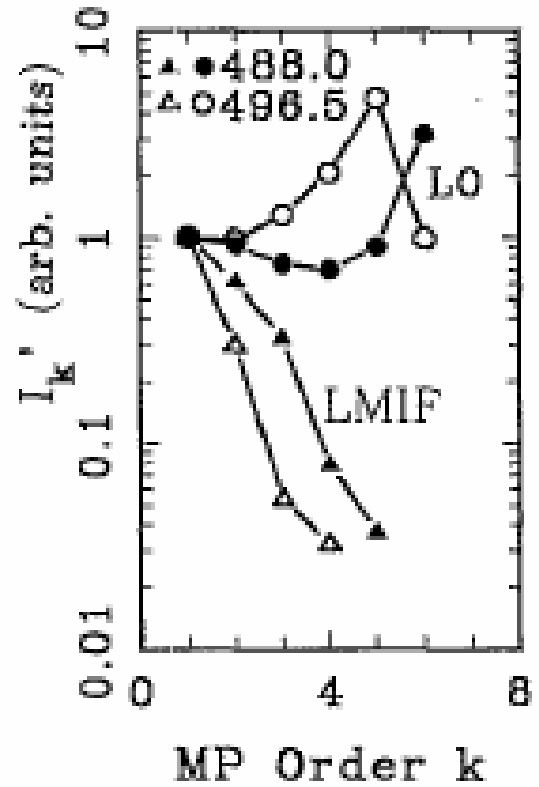
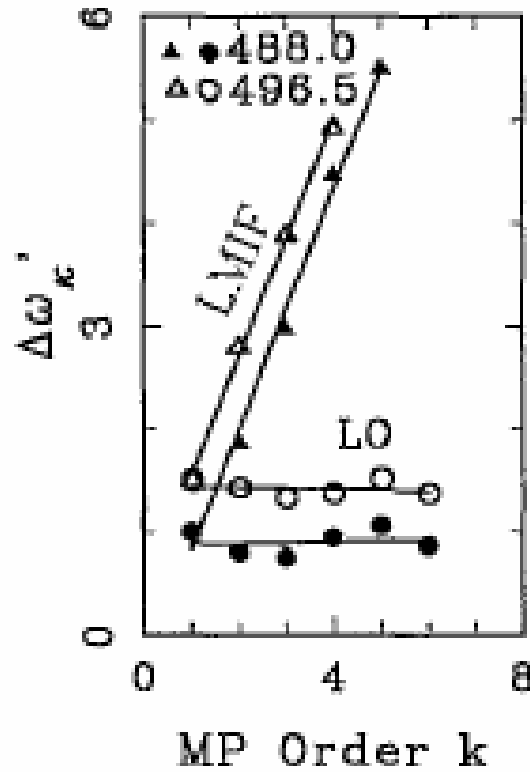
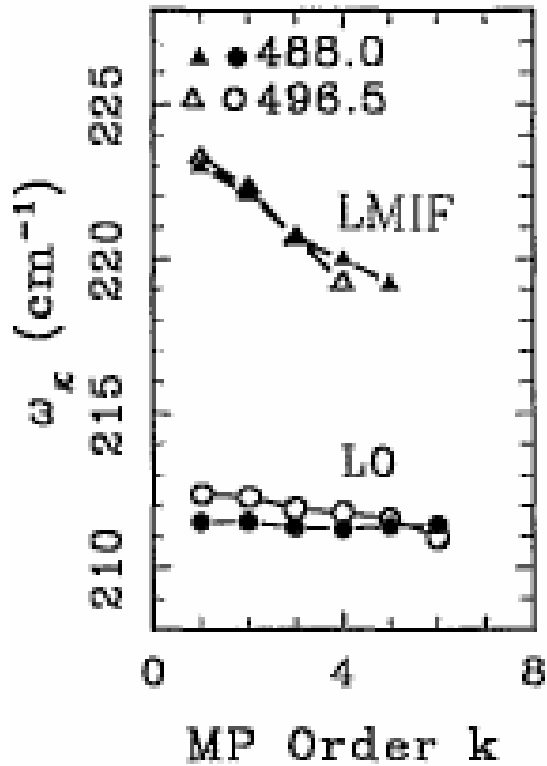
$$\Delta\omega_k = k\Delta\omega_1 \sim \Delta\omega_k / k = \Delta\omega_1$$

- Intensity

$$I_k < I_{k-1}$$

A. Superlattices

1. Sample: $(\text{CdSe})_4/(\text{ZnTe})_4$ SLs
2. Observed results of micro-IF MP modes



2. Interpretation

We note a paper:

PHYSICAL REVIEW B

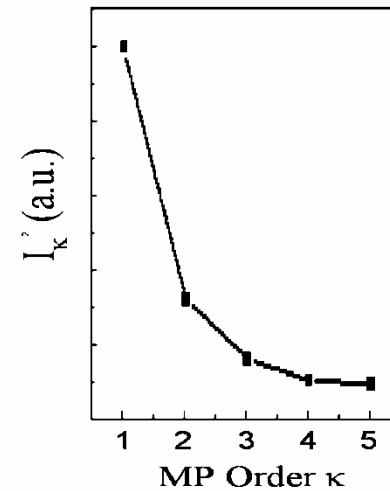
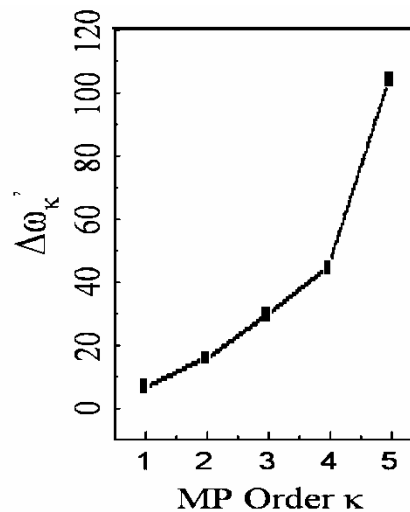
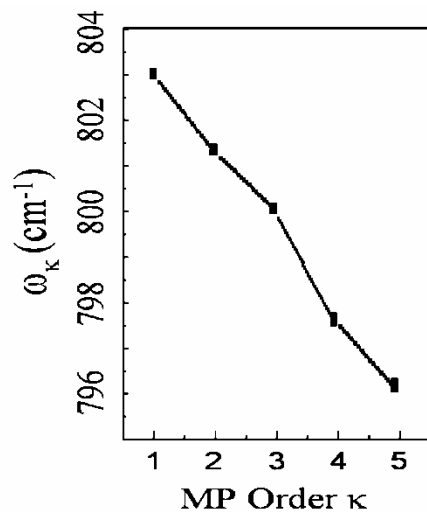
VOLUME 15, NUMBER 2

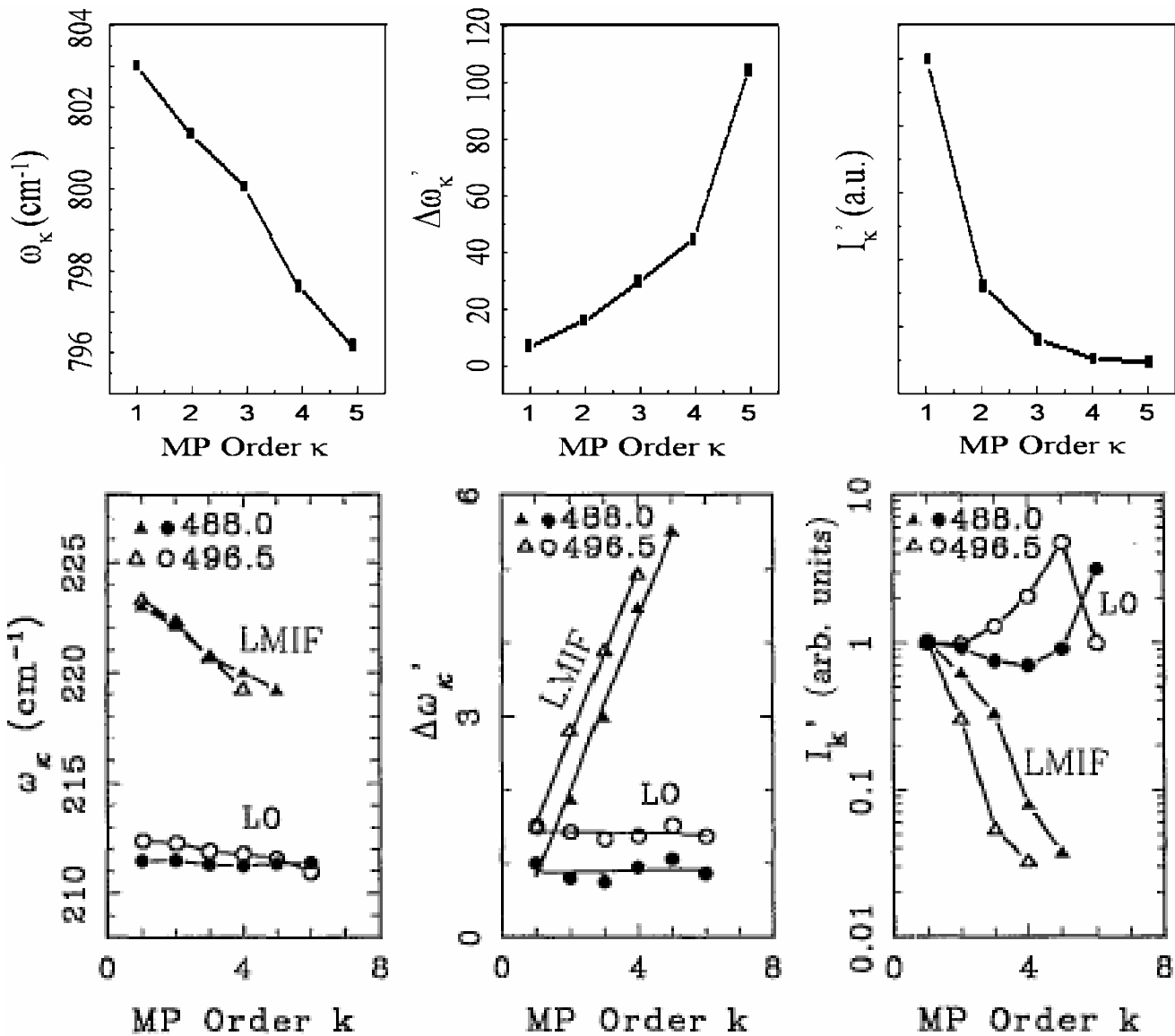
15 JANUARY 1977

Multiple-order Raman scattering in MnO_4^{2-} -doped CsI

T. P. Martin and S. Onari[†]

Max-Planck-Institut für Festkörperforschung, Stuttgart, Federal Republic of Germany

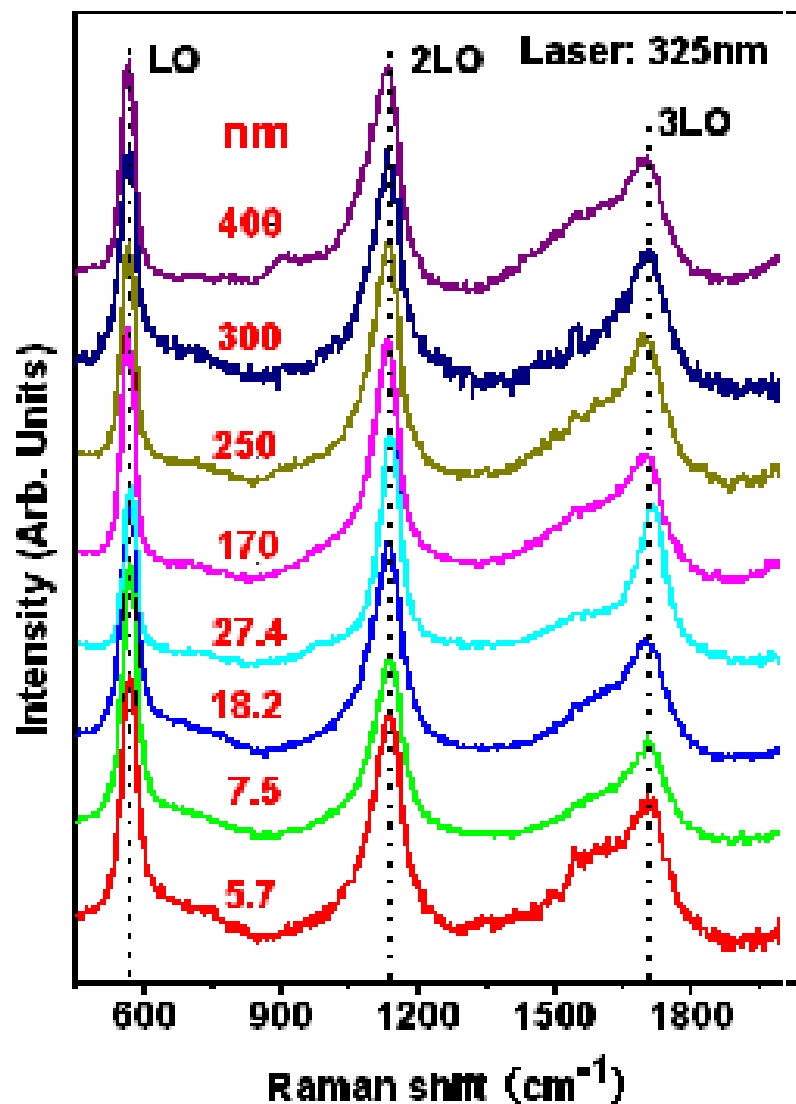




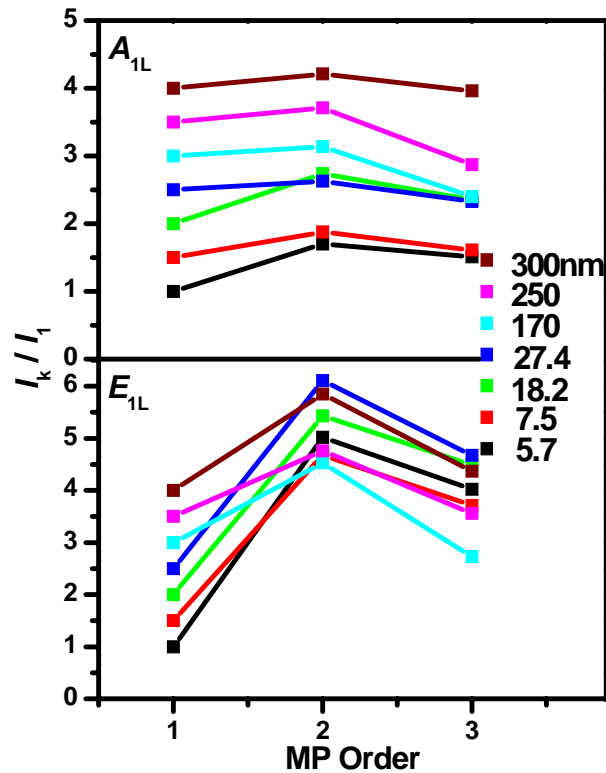
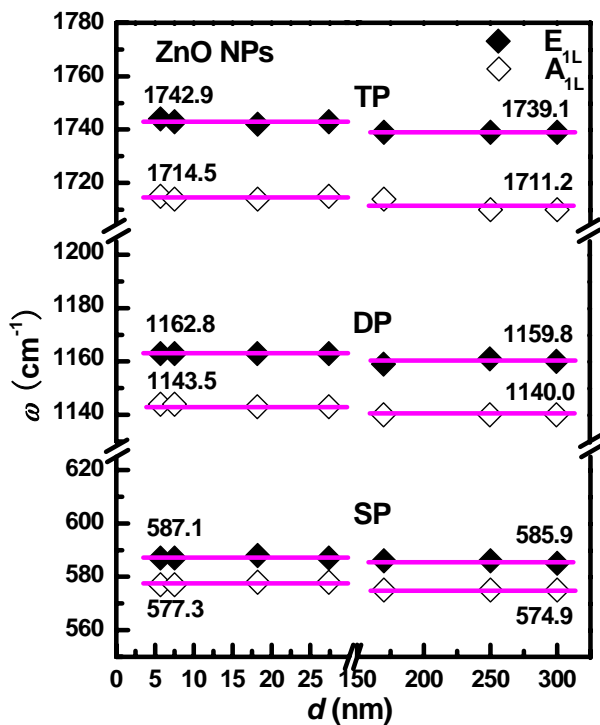
- ❑ Interface in SLs is a defect-like;
- ❑ SLs is a defect-like structure

B. Nano-matrerials

1. MP Raman spectra of ZnO NPs



Dependence of MP Raman frequency and intensity on sample sizes



Observed

$$\omega_k = k\omega_1$$

$$I_3 < I_2 > I_1$$

The predication of MP Raman features:

- The Raman frequency of higher order k phonons, ω_k , should be integral times of the frequency of first order phonon ω_1 :

$$\omega_k = k\omega_1.$$

- The Fröhlich coupling constant in nano-crystals is smaller than one for nano-crystals and the intensity of MP relation should be expected

$$I_{R,1} < I_{R,2} > I_{R,3}$$

However, they **violate the traditional view** of MP Raman spectra:

$$\omega_k \neq k\omega_1$$

$$I_{R,1} > I_{R,2} > I_{R,3}$$

Brief summary

- In the features of frequency, selection rule and ensemble spectra, we have found some abnormal features that violates the features and understanding of present nanostructure Raman spectroscopy.
- In the interpretation of above abnormal phenomena, abnormal frequency and amorphous features still not get a reasonable interpretation, although the others has found to be ascribed the defect-like and super-thin structures of samples.

In the next part we will concentrate to discuss their origin and nature

IV-4 The origin of above novel features

Note:

- No RRSE and NFSE mentioned above **is limited in ZnO NPs.**
- The suggestions are all based on the Raman spectroscopy of present nanostructures and theory.

To obtain a reasonable origin and nature, it is needed having;

- A much **more experimental facts** to obtained regular pattern of NRSSE and NFSE.
- Giving up traditional idea to found interpretaion.

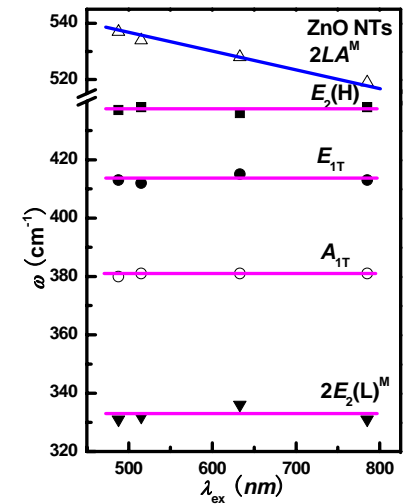
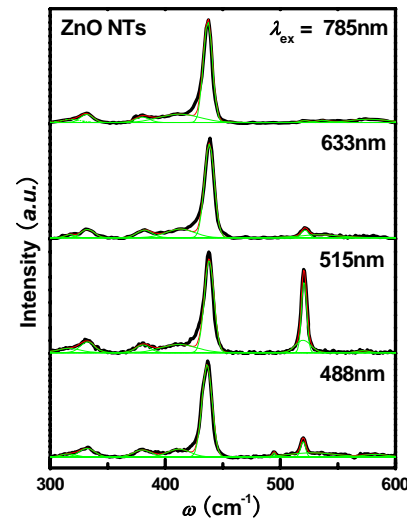
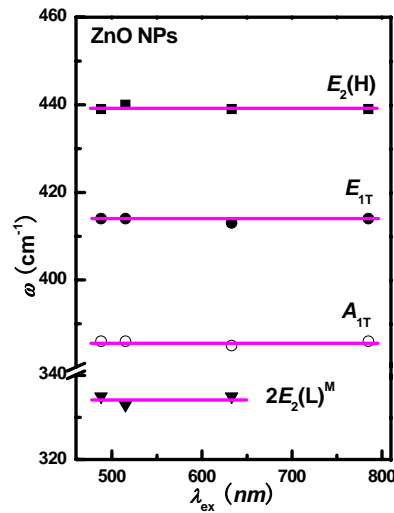
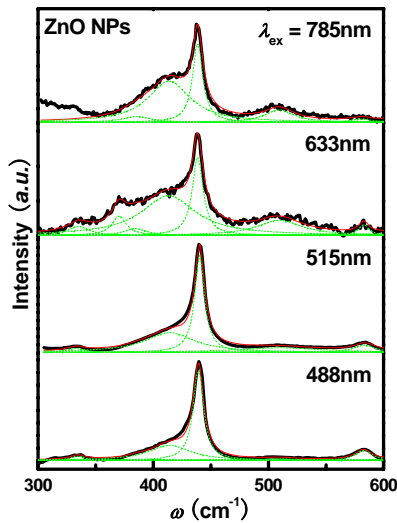
(I) Regular pattern of RSSE and FSE

1. Observed results

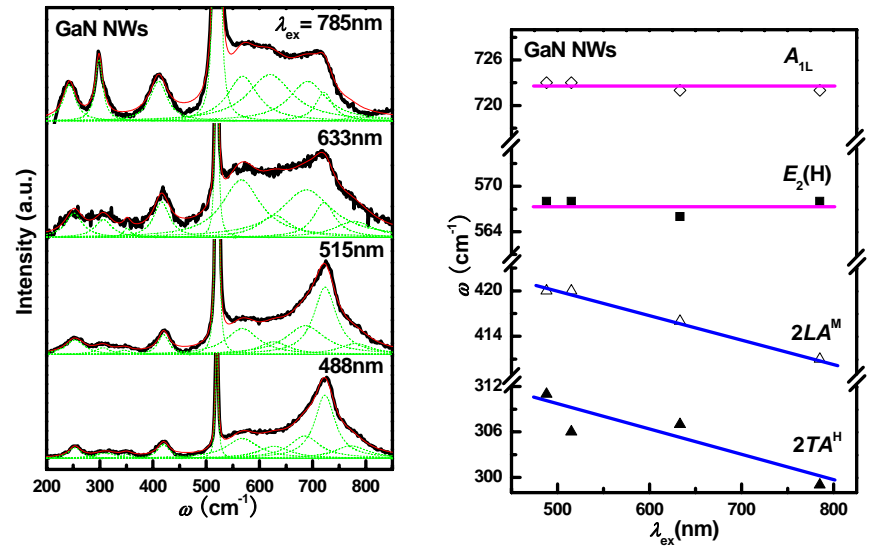
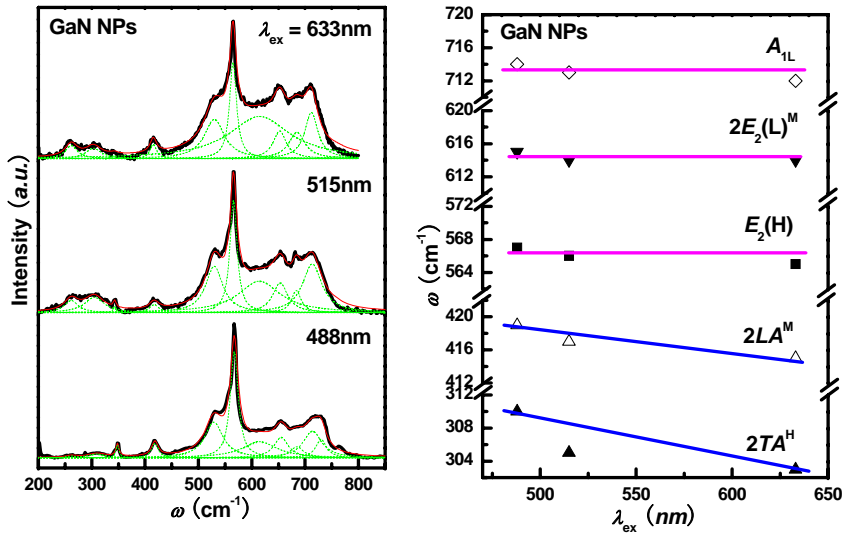
(1) Optical Phonons

RSSE

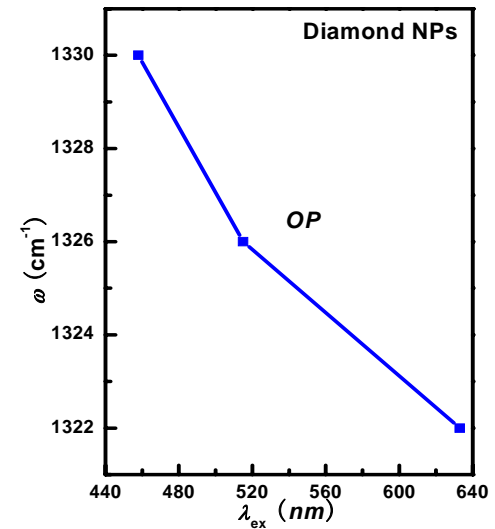
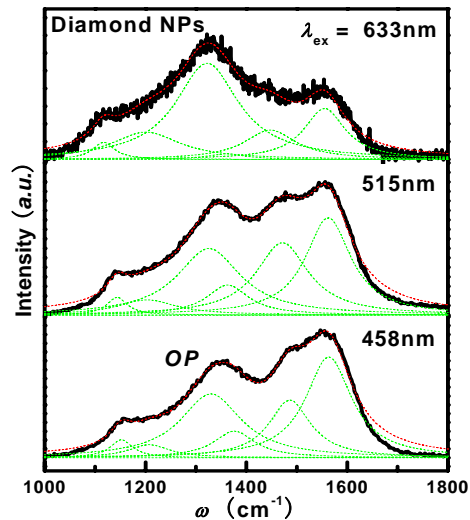
● ZnO nanoparticles and tubes



● GaN nanoparticles and wires

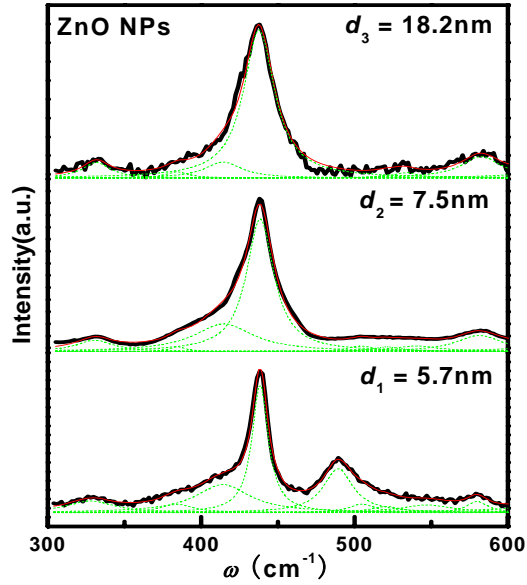


● Diamond nano-particles



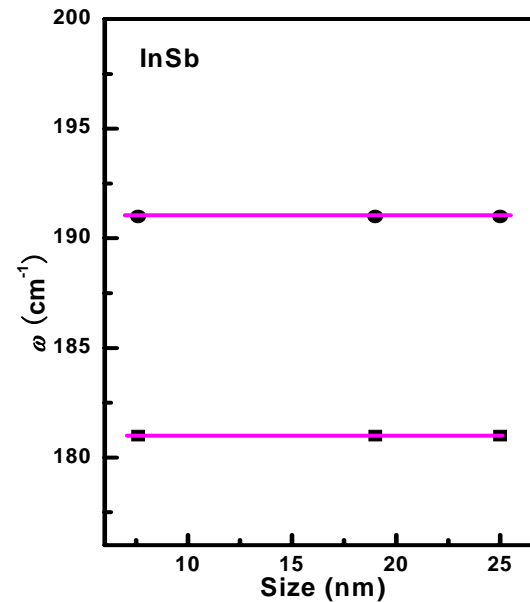
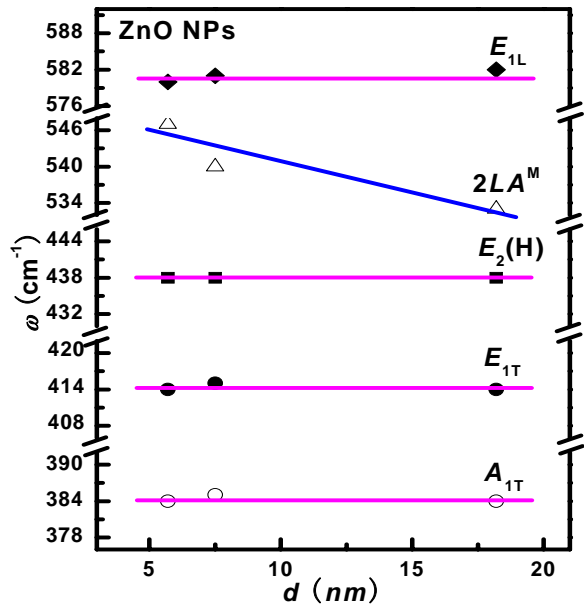
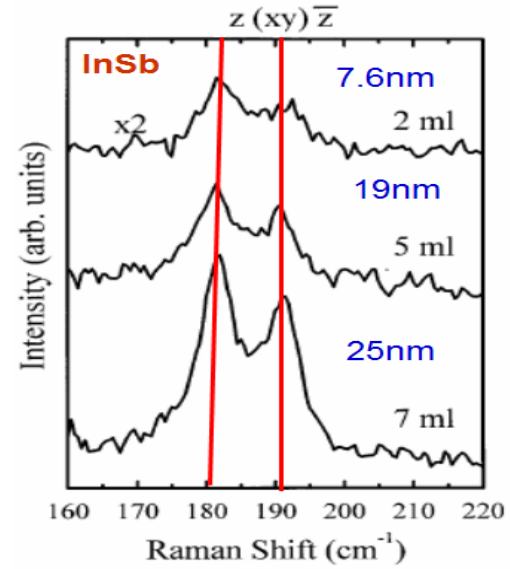
FSE

ZnO NPs

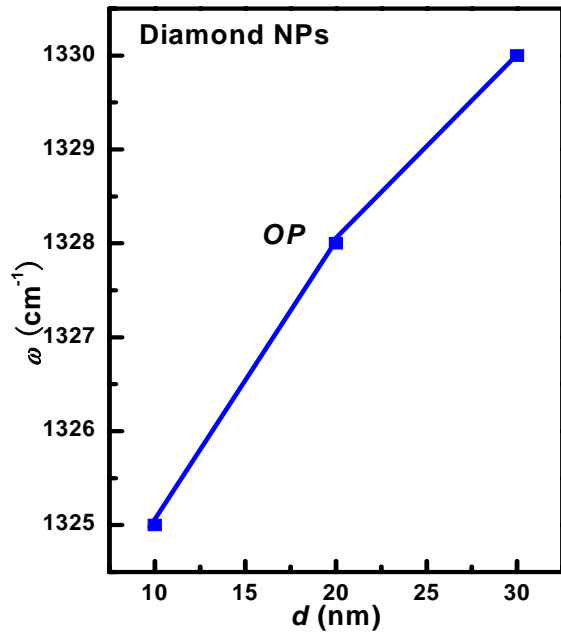
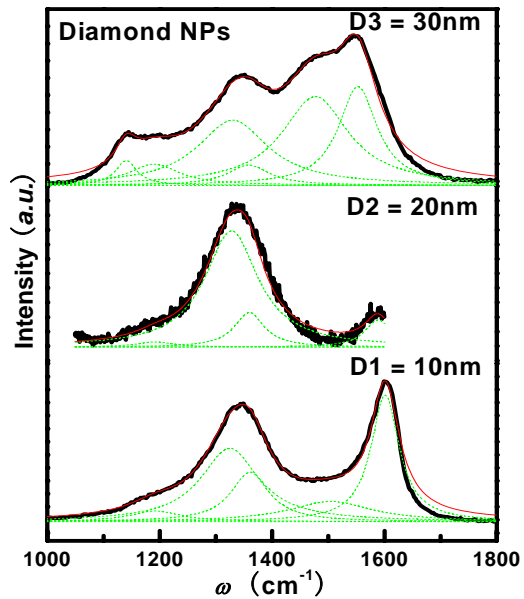


InSb NPs

-Armelles, 81(1997)6339

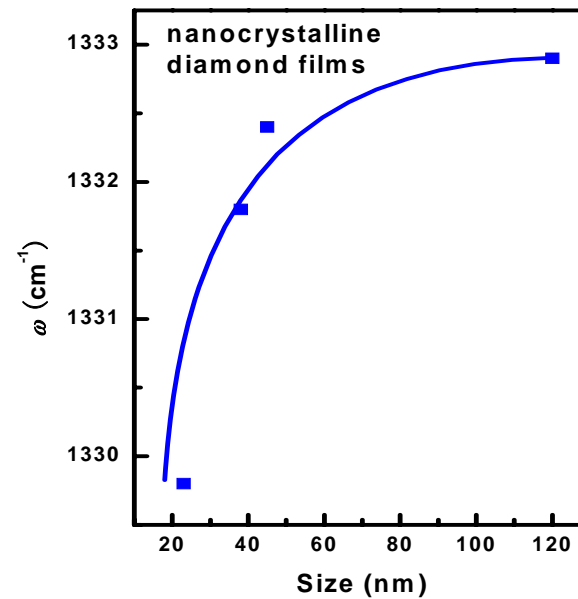
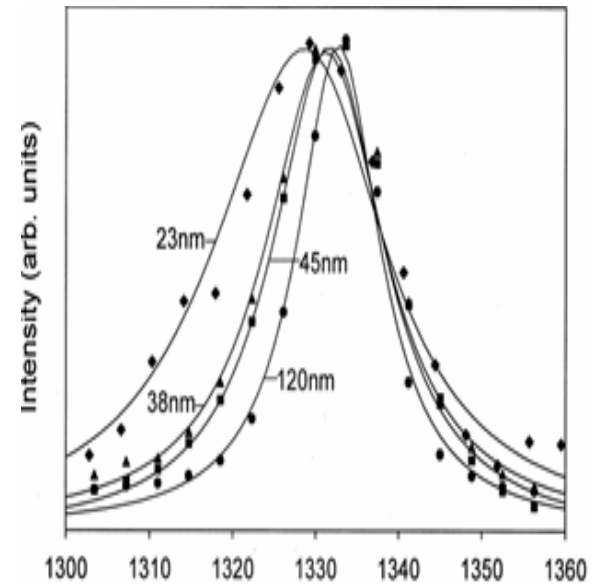


Diamond NPs



Diamond NCs

-Z. Sun et al. DRM, 9(2000)1979



(2) Acoustics phonon

● CdSe NRs

-H. Lange, et al, Nano Lett., 8(08)4614

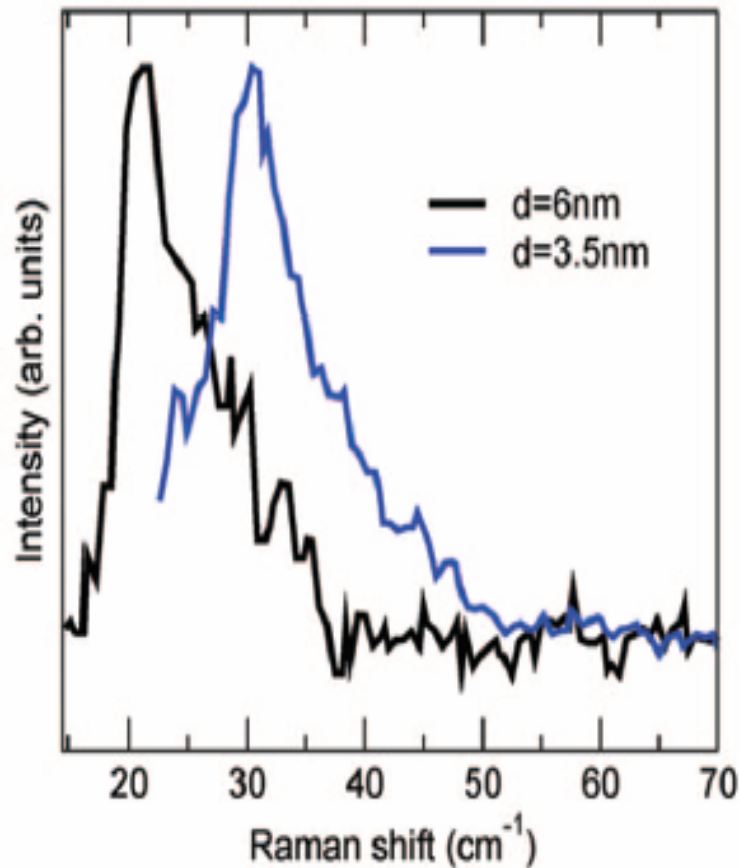
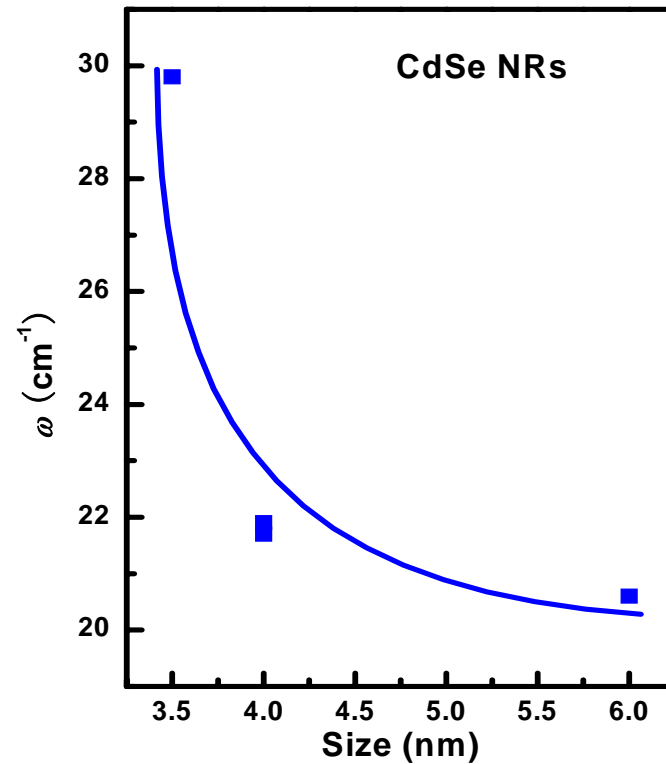


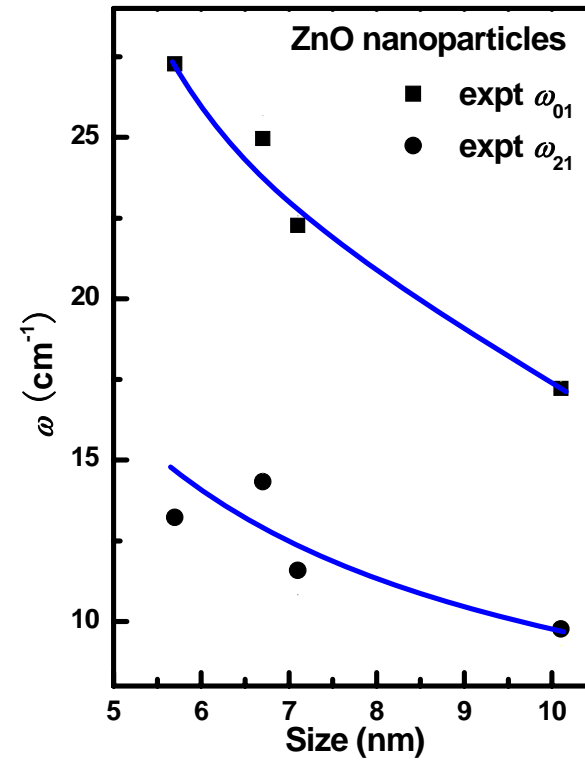
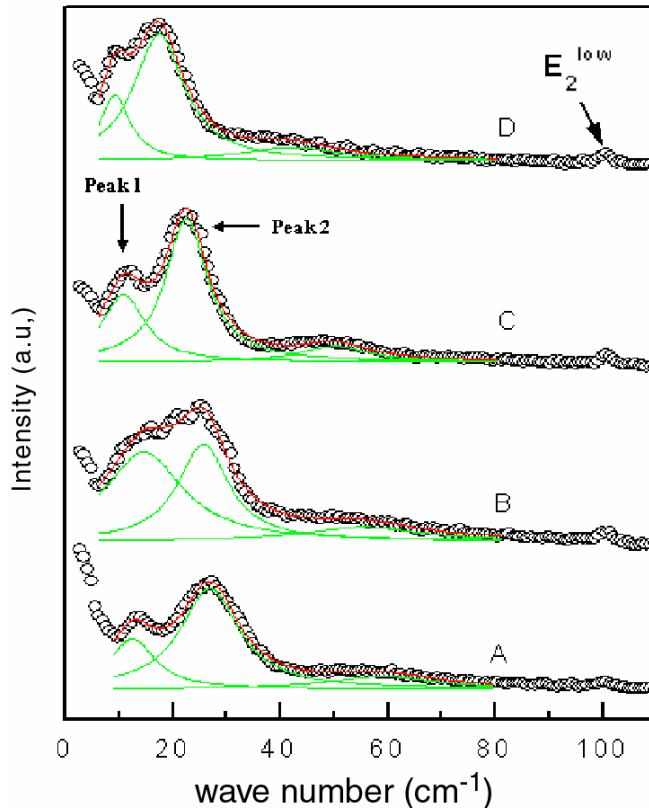
Table 1. Radial Breathing Mode Frequency of CdSe Nanorods

sample dimensions	$\omega_{\text{RBM}}, \text{cm}^{-1}$
3.5 nm \times 20 nm	29.8
4 nm \times 25 nm	21.9
4 nm \times 30 nm	21.7
6 nm \times 35 nm	20.6



● ZnO nanoparticles

- Harish Kumar Yadav, PRL. **97**, 085502 (2006).



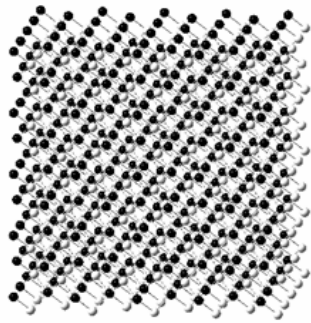
(II) Calculated regular patten

● Atomic structure in cluster model

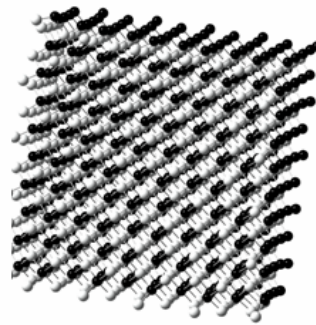
ZnO/InSb



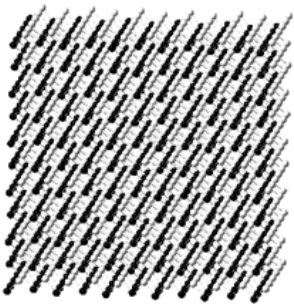
Atoms: 512



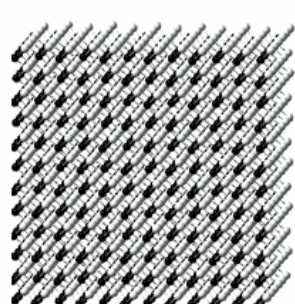
730



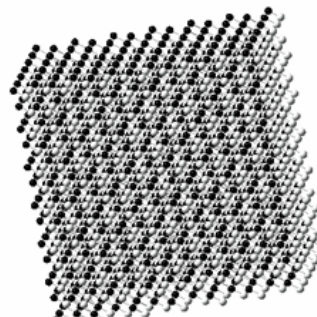
1000



Atoms: 1332



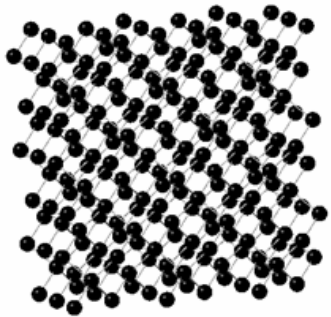
1728



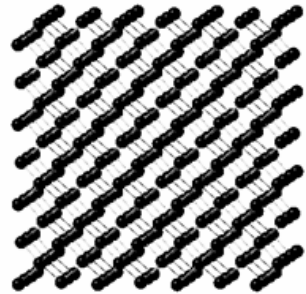
2198

Atom Number	Sizes (nm)	
	ZnO	InSb
512	2.12	2.42
730	2.40	2.75
1000	2.69	3.07
1332	2.97	3.39
1728	3.25	3.72
2198	3.53	4.04

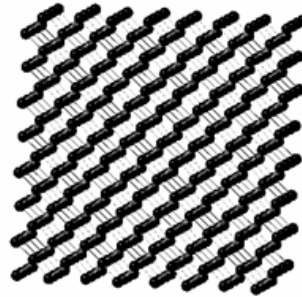
Si / diamond



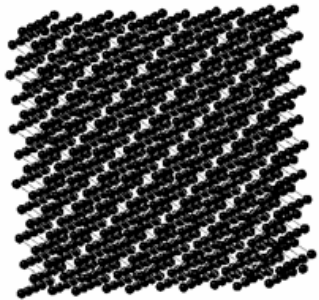
Atoms: 216 atoms



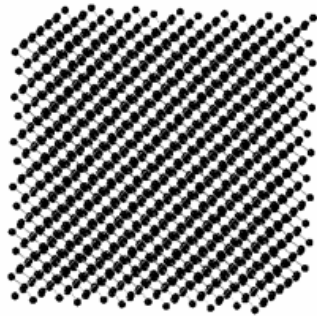
344



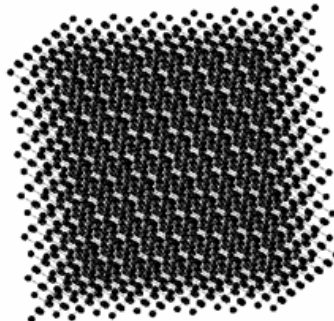
512



Atoms: 1000



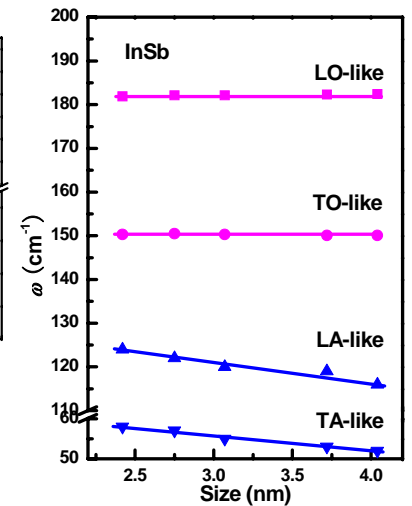
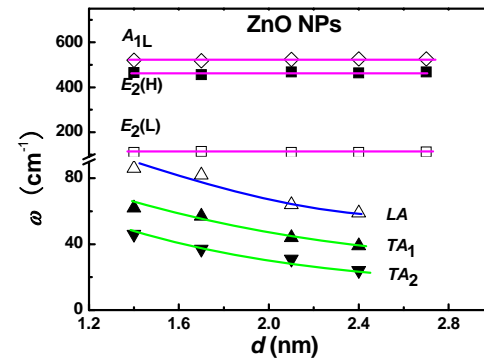
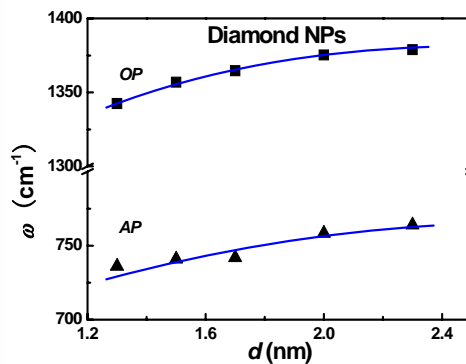
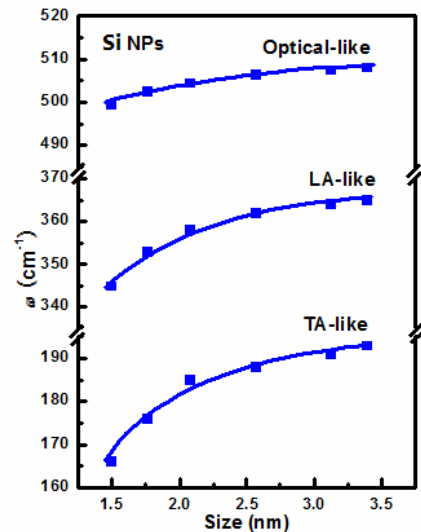
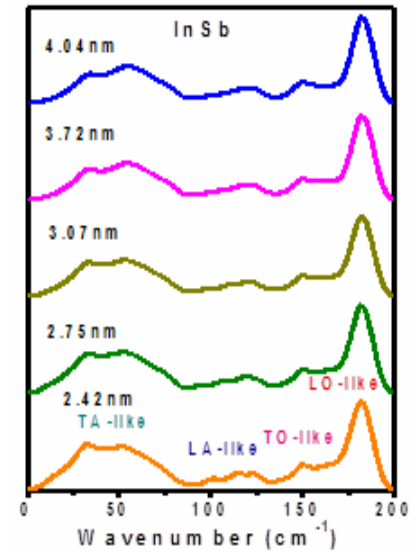
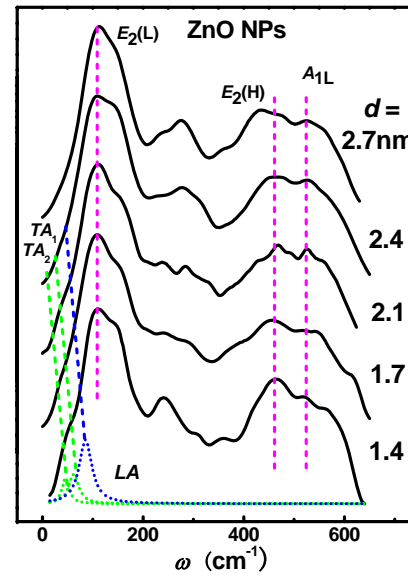
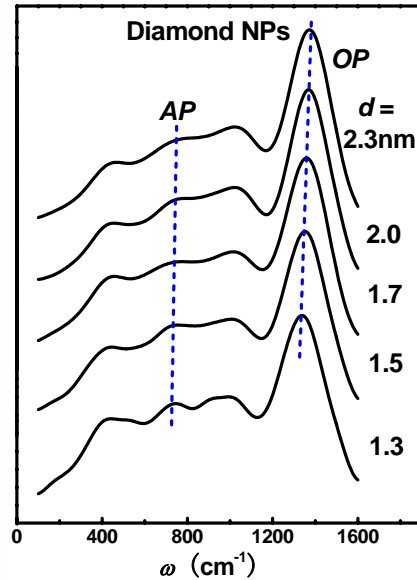
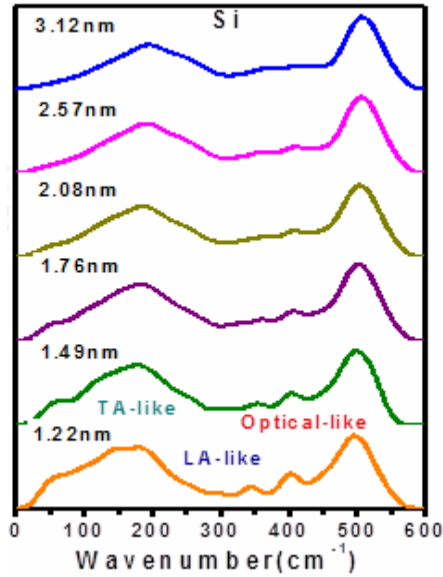
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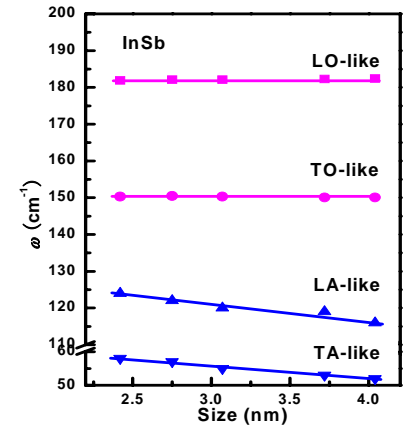
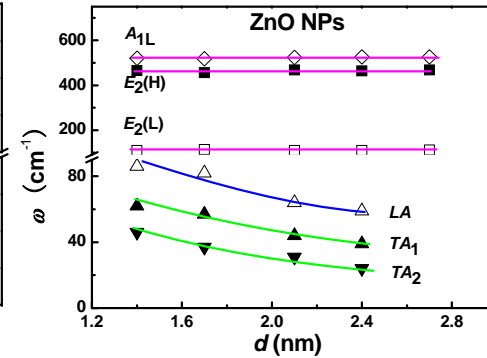
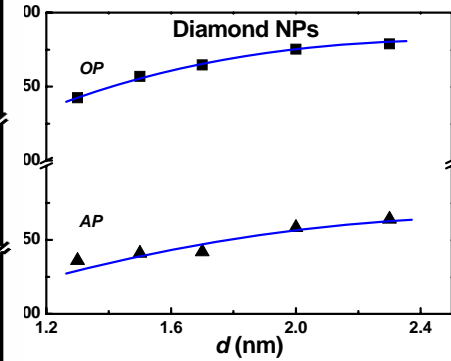
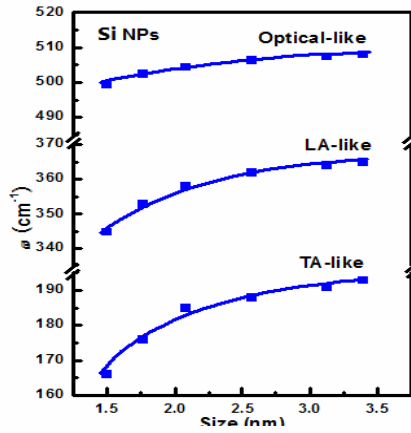
2198

Atom number	Sizes (nm)	
	Si	diamond
216	1.49	0.98
344	1.76	1.16
512	2.08	1.34
1000	2.57	1.69
1728	3.12	2.05
2198	3.39	2.23

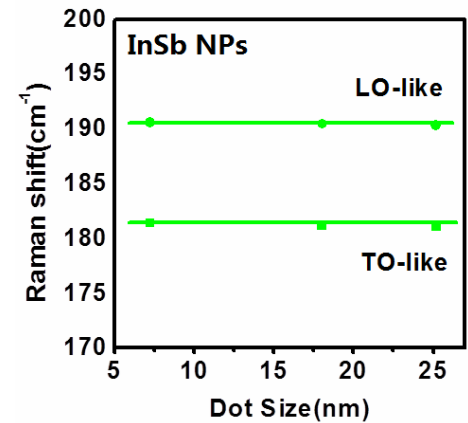
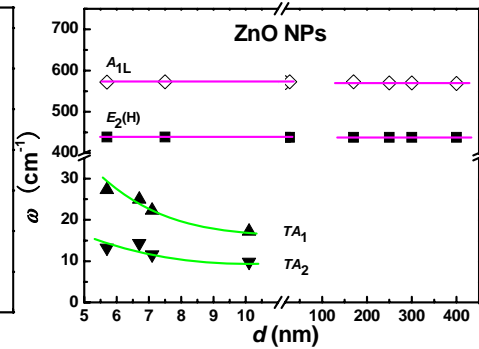
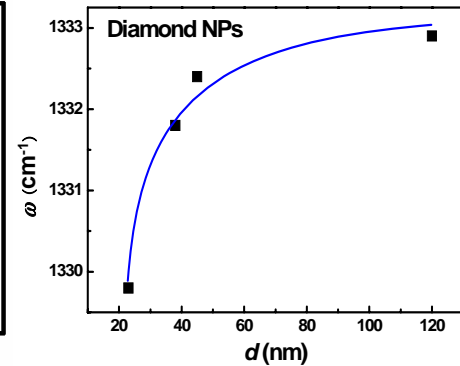
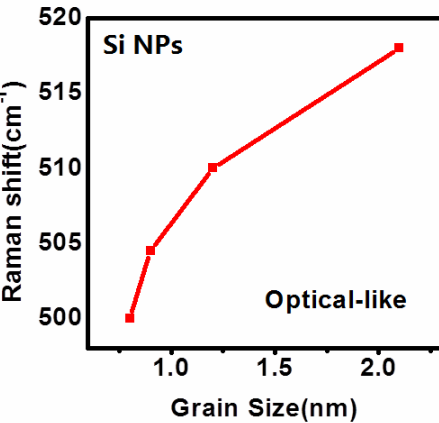
Calculated spectra and frequency dependence on sizes



Calculated results



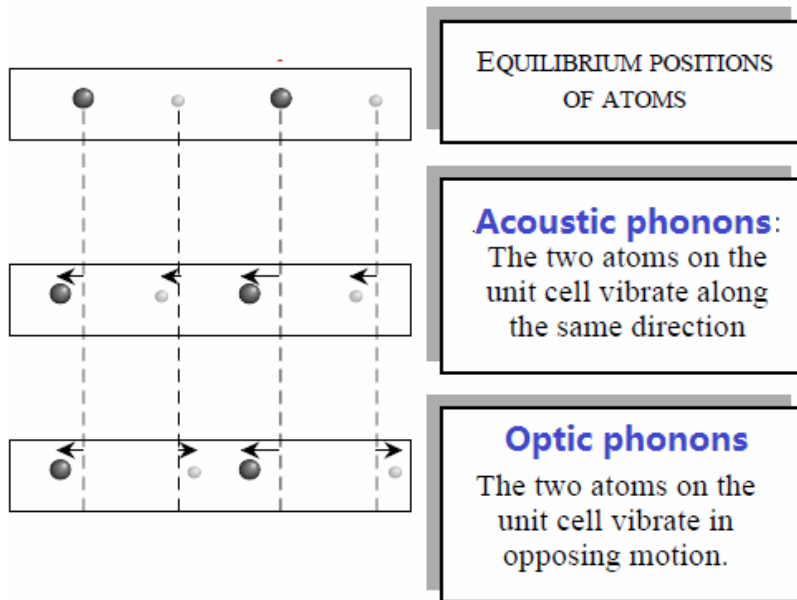
Observed results



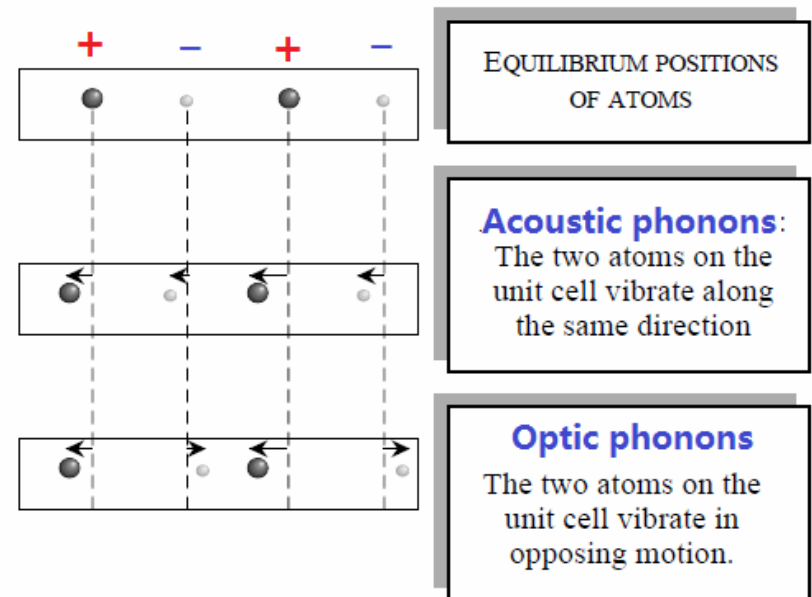
Calculated results Match observed results, Both show:

- The optic phonons of polar nano-semiconductors:
No FSE.
- The optic phonons of non-polar nano-semiconductors and all of acoustic phonons of nano-semiconductors:
Do FSE.

Non-polar semiconductors



Polar semiconductors



1. non-polar semiconductors
polar semiconductors
2. Acoustic phonons
Optical phonons

electric neutrality
ionicity
Deformation (no charge)
interaction
Coulomb (Fröhlich)
interaction added

In the calculation:
Do and **Not** to take account of the **charge**
for **polar** and **non-polar** samples, respectively.
Charges play a key role!

Existence of Positive and negative charges



- In matters, have a long range Coulomb potential
- In phonon systems, appear a
long range electron-phonon (Fröhlich) interaction

The No FSE may be originated from
Fröhlich interaction.

It should be confirmed!

The predication of MP Raman features:

- The Raman frequency of higher order k phonons, ω_k , should be integral times of the frequency of first order phonon ω_1 :

$$\omega_k = k\omega_1.$$

- The Fröhlich coupling constant in nano-crystals is smaller than one for nano-crystals and the intensity of MP relation should be expected

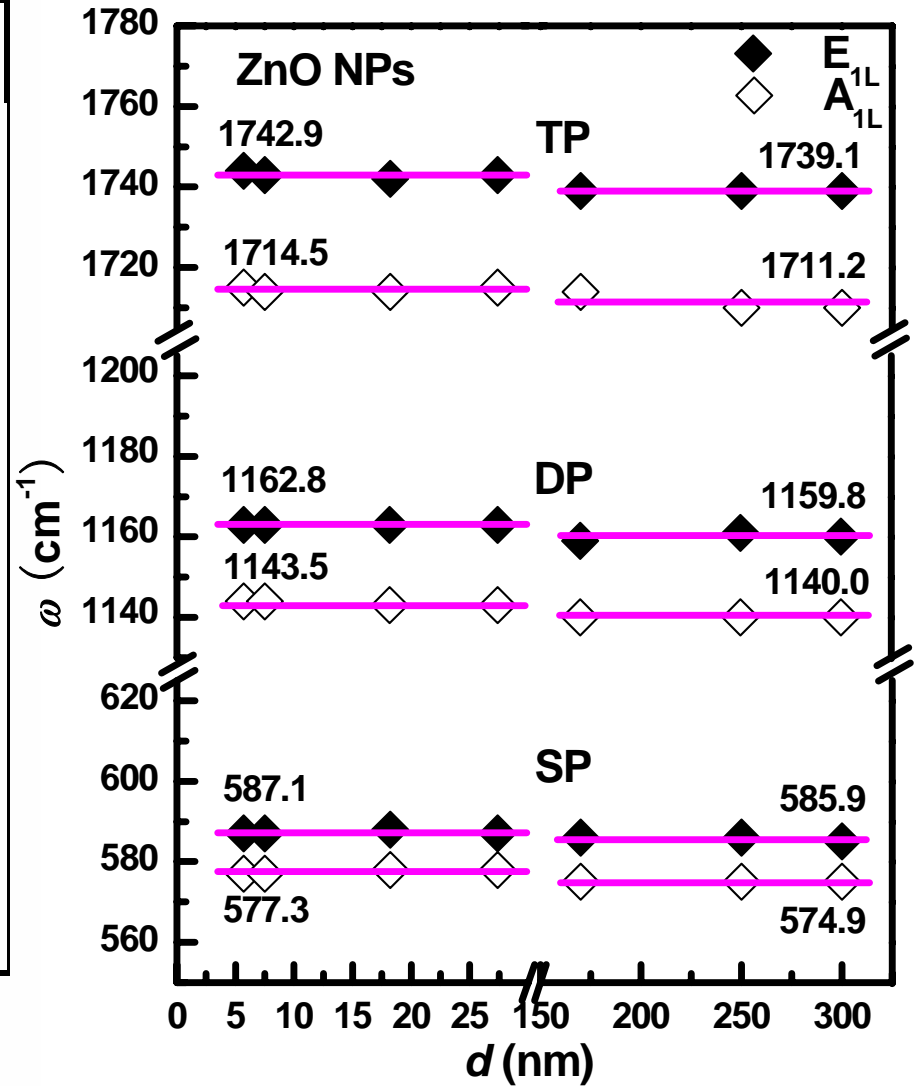
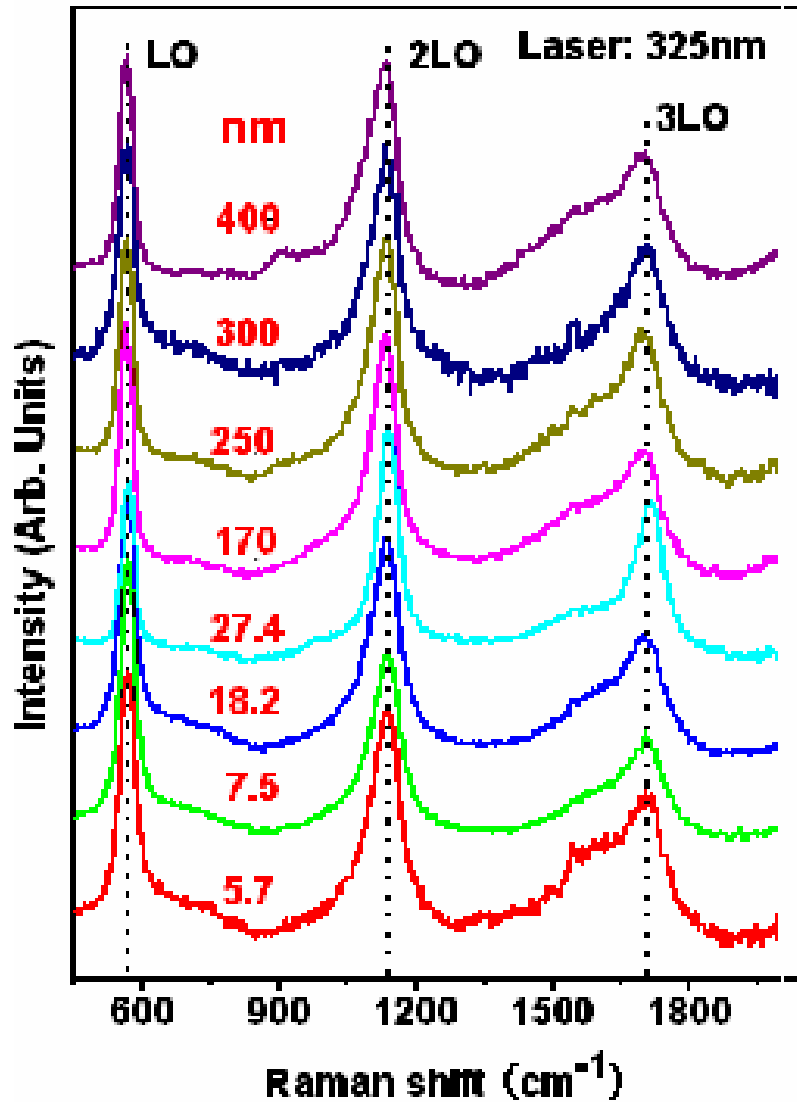
$$I_{R,1} < I_{R,2} > I_{R,3}$$

However, they **violate the traditional view** of MP Raman spectra:

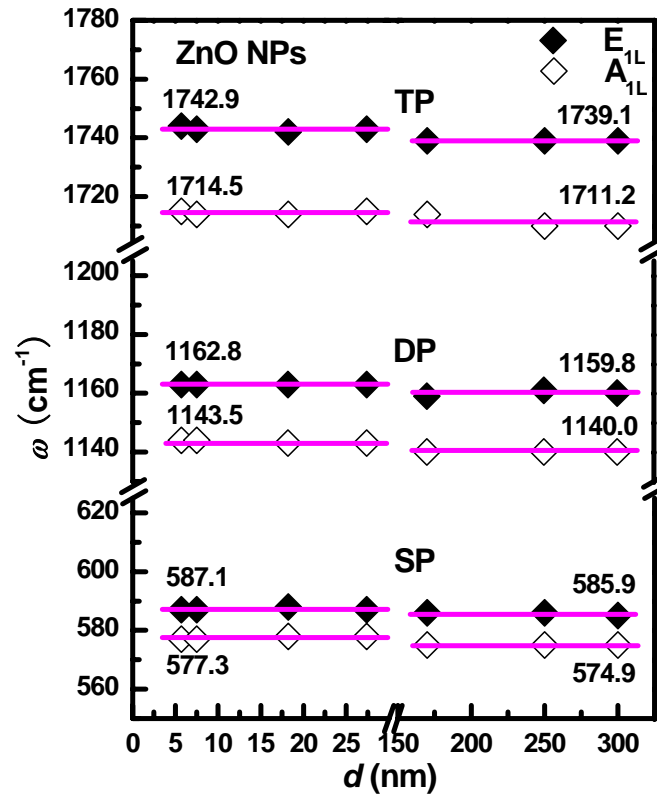
$$\omega_k \neq k\omega_1$$

$$I_{R,1} > I_{R,2} > I_{R,3}$$

2. Confirmation by MP Raman spectra of ZnO NPs



Feature 1: Dependence of MP Raman frequency ω_{Obs} of A_{1L} and E_{1L} mode on sample sizes



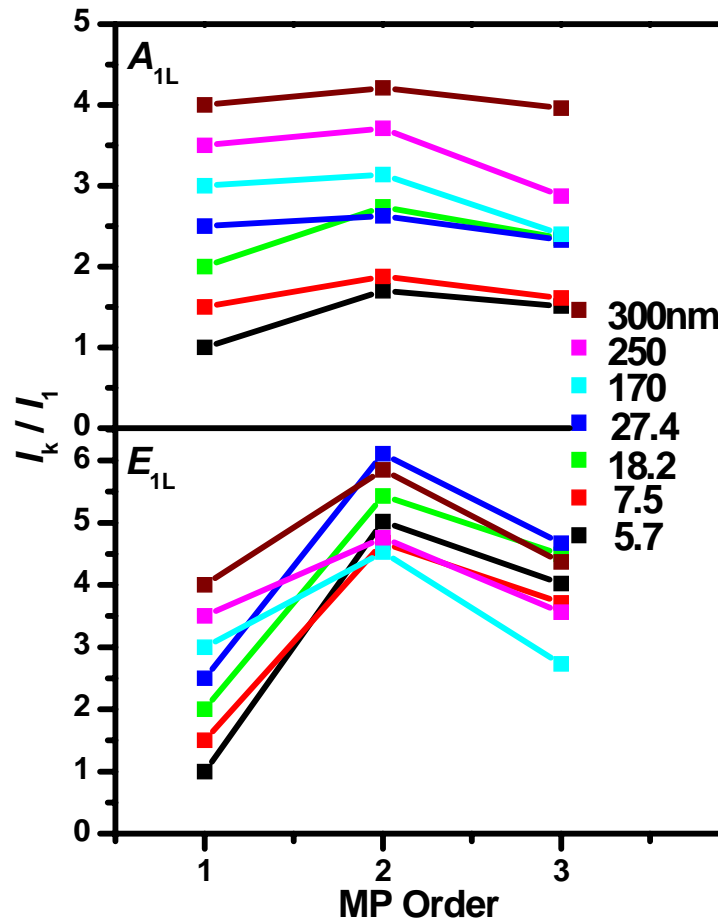
Observed

$$\omega_k = k\omega_1.$$

Confirm the role of Fröhlich interaction

Dependence of relative intensity I_k/I_1 of A_{1L} and E_{1L} mode on MP order k .

$$I_3 < I_2 > I_1$$



Confirm again the role of Fröhlich interaction

(II) Confirmation of suggested origin

1. Fröhlich interaction H_F and predication for Raman spectra

H_F with phonon wavevector q and the sample volume V can be expressed as approximately²¹

$$H_F \sim q^1 V^{1/2}$$

- At $q \approx 0$ of the Brillouin zoon, Fröhlich interaction plays a key role.
- Since the V of nano-semiconductors is very small, H_F will be critical.



For **frequency** of single and multiple phonon:
the scattering of OPs in polar nano-semiconductors
occur at $q \approx 0$ only

No FSE!

For **intensity** of multiple phonon: The abnormal
has been interpreted **successfully in terms of**
Fröhlich interaction by Rodríguez-Suárez, et al.
-Multiphonon resonant Raman scattering in
nanocrystals, *Phys. Rev. B* **62**, 11006-11016 (2000).]

IV-5 Nature of above novel features

Active range of Fröhlich interaction is
10 times of lattice constants ~ 50 nm.



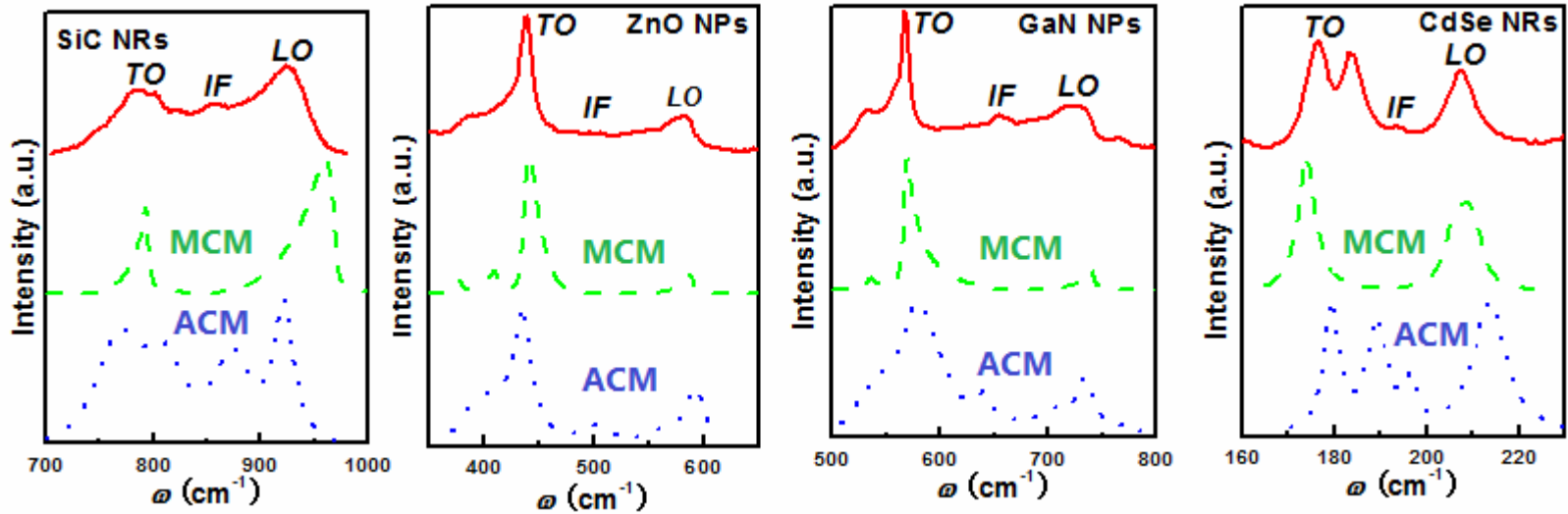
In optic phonon system polar NC-semiconductor:
No long-range order

No long-range order

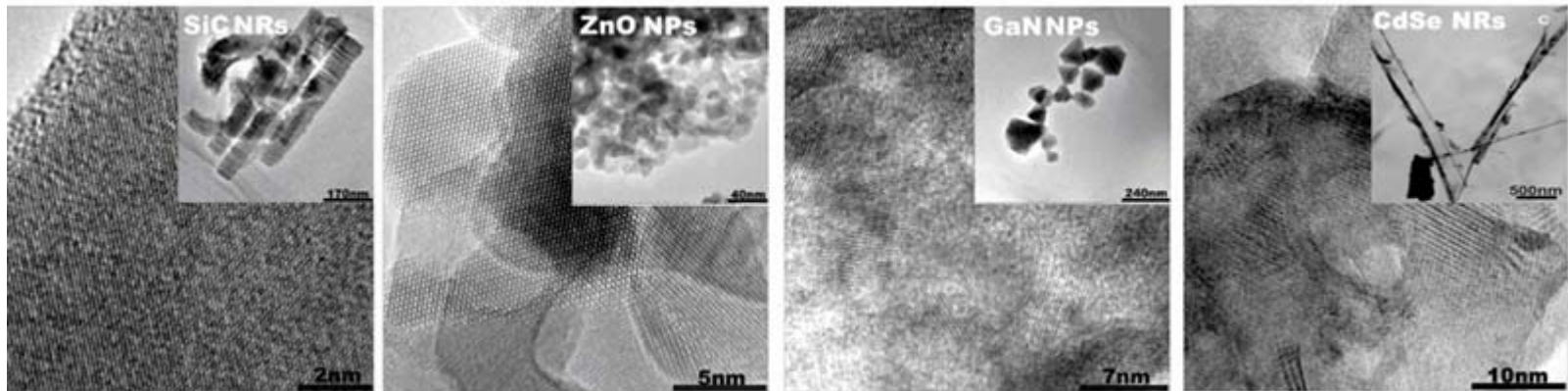


- Translation symmetry **breaking!**
- Raman spectra must be **amorphous!**

Raman spectra are amorphous



Samples are crystalline



Origin and nature are confirmed !

Summery-New Physics

A. On Structure

A perfect nanostructure can be the defect one intrinsically.

●CNTs: $\Delta = |\omega_{As}| - |\omega_s| \neq 0$

●SLs: In (CdSe)₄/(ZnTe)₄ SLs, abnormal dependence of micro-IF MP Raman spectra with MP order.

B. On FSE

● For same size of NPs, different elementary excitations have FSE or no FSE. Such as, in ZnO NPs,

Electron and phonon; Optic and acoustic phonons.

In fact, it is the issue related with characteristic lengths.

● For different barrier size of SLs have FSE or no FSE. Such as, Abnormal selection rule of IF Mode of (GaAs)₄/(AsAl)₂ SLs.

C. On Spectral Ensemble Feature

For optic phonons of polar nano-semiconductors.

The Raman spectrum of crystals appears amorphous feature!

D. On Symmetry

In crystalline nanostructure

Some sub-system can be translation symmetry.

Such as optical phonon system of polar nano semiconductors.

E. On Fröhlich Interaction.

In nano-structure

Fröhlich interaction plays a distinct and crucial role.

which has been verified to be the origin of abnormal phenomena appeared in OPs of polar nano-semiconductors.

Acknowledge:

National Basic Research Program of China (973 Program) under grants No. 2009CB929403;
NSF of China under grants Nos. 10774006 and 60876002;
RGC of Hong Kong under Grant No. 401003;
NCS of Taiwan;
All people joined the research related to the objects.

